A STATISTICAL STUDY FOR AUTOMATIC CALIBRATION OF A CONCEPTUAL RUNOFF MODEL

STATISTISK STUDIE FÖR AUTOMATISK KALIBRERING AV EN BEGREPPSMÄSSIG AVRINNINGSMODELL

Sören Svensson

SMHI Rapporter

HYDROLOGI OCH OCEANOGRAFI Nr RHO 10 (1977)

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SUMMARY

A conceptual runoff model is studied in this work. Especially the residuals of the model (the differences between the computed hydrograph and the recorded one) are examined. The density function and the autocorrelation function of the residuals are estimated and tested.

The model must be calibrated for each new catchment, to which it is applied. Therefore a criterion of the goodness of fit between the computed and the recorded hydrograph is required. Some criteria of fit have been examined concerning their sensitivity to changes in the model parameter setting.

Conclusions of the work are: The residuals of the model are neither stationary nor independent and normally distributed. A classification based on the different physical processes, which govern the discharge, makes the residuals of each class more stationary and in some sense more normally distributed than the residuals of the material without any classification. Furthermore a criterion of goodness of fit, based on the classification above resembles the subjectively judged fit more than the simple sum of squares criterion, which has become practice in applications of runoff models.

1. INTRODUCTION

The purposes of the development of hydrological catchment models are mainly (Clarke, 1973):

- 1. Forecasting
 - a) Operational forecast: Estimating streamflow when rainfalls, losses, streamflows etc. are given up to the present time.
 - b) Design forecast: Estimating the flood hydrograph caused by a hypothetical heavy storm (or snowmelt).
- 2. Extending the discharge redord, where we have got long climatological record but short discharge record.
- 3. Prediction of the possible effects of proposed physical changes to the catchment.

Before the model can be taken into operation, its free parameters have to be accurately estimated by means of a calibration procedure. This means that the parameters are adjusted until a good fit is obtained between the computed hydrograph and the observed one. The procedure can be either a subjective one, relying upon the hydrologist when deciding which parameters are to be adjusted, or an automatic one, based on an optimization algorithm.

One major problem concerning the automatic procedure has been the finding of a matching index, a criterion of fit. This is very important, because every automatic parameter optimization routine has to rely upon a numerical value of the goodness of fit between two curves.

The statistical properties of the residuals could be a key to a better understanding of this problem. The lack of such studies was pointed out by Clarke (1973).

Clarke (1973) also stated that if estimated confidence regions for the parameters are required, assumptions must be under about the probability distribution of the model residuals. However, one further possibility is to do a number of parameter estimations based on independent data and from the results of these estimations get an apprehension of the size of the confidence regions of the model parameters.

The aim of this work is to study the statistical properties of the residuals in order to find a more appropriate criterion of fit between the computed and the recorded hydrograph. This problem was approached in two steps.

- 1. The calibration period was divided into "subperiods" in order to obtain stationary subsets of residuals. Some statistical properties of these residuals were examined.
- 2. The response surfaces of different criteria of fit were studied when altering the parameter values.

The HBV runoff model was used for the study. This model is developed at the SMHI (Swedish Meteorological and Hydrological Institute) by Bergström (1976). It is in operational use in some catchments in Sweden and Norway.

This study was financed by the SMHI and it was carried out in co-operation with the Department of Mathematics at the Lin-köping University,

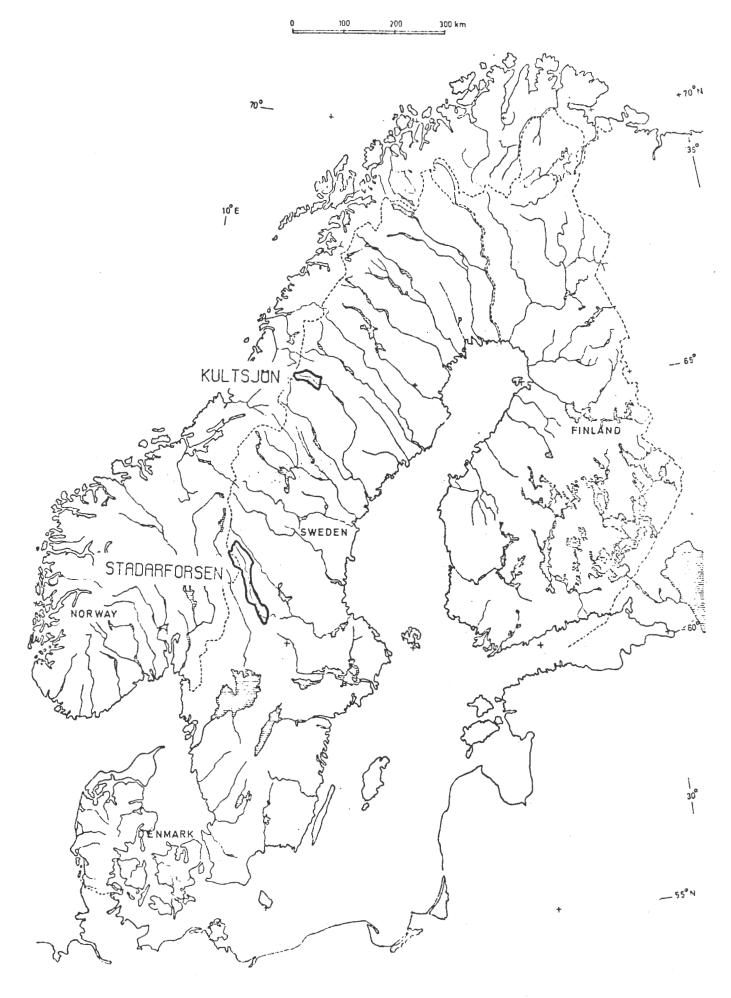


Fig. 2.1. Test catchments for the applications of the study of the HBV model.

2. TEST CATCHMENTS

Two catchments were used in the study: the Kultsjön catchment, below referred to as Kultsjön, and the Stadarforsen catchment, below referred to as Stadarforsen (fig. 2.1). Both catchments are below timberline dominated by coniferous forest, and the soil is mostly moraine or of a pervious type.

The catchments are representative for large areas in Scandinavia.

Table 2.1 Test catchments.

| Catchment | River | Area (km²) | Altitude range (m) | Lakes % |
|--------------|----------------|---------------|--------------------|------------|
| Stadarforsen | Västerdalälven | 4 136 | 835 | 2,4 |
| Kultsjön | Ångermanälven | 1 109 | 1 040 | 6 |

The analysed runoff record of Stadarforsen began 1961-10-01 and ended 1976-03-31. In Kultsjön the analysed record began 1961-10-01 and ended 1976-05-18.

3. THE HBV-MODEL AND ITS FREE PARAMETERS

The simulation of discharge by the HBV-model is made in three steps (fig. 3.1).

- 1. Snow accumulation and ablation.
- 2. Soil moisture accounting.
- 3. Generation of runoff and transformation of the hydrograph.

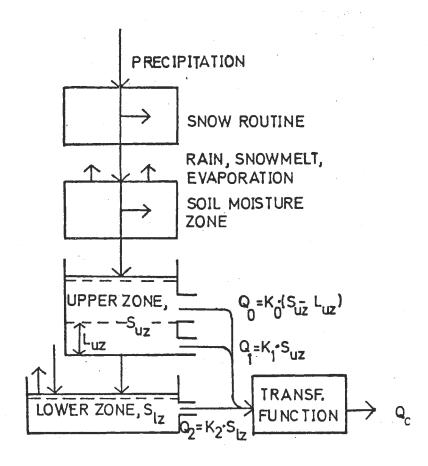


Fig. 3.1 Schematic representation of the HBV-model.

Table 3.1 Parameters of the HBV-model.

Corrections on input variables

P = correction factor on rainfall

P_{lapse} = precipitation-elevation correction

= temperature-elevation correction

= general temperature correction

Parameters of the snowroutine

Csf = snow fall correction factor

= degree-day melt factor

= water holding capacity

= bottom storage under snowpack

 $^{\mathrm{C}}$ rfr = refreezing coefficient

Parameters of the soil moisture routine

= maximum soil moisture storage Fc

= limit for potential evaporation L_{p}

= empirical coefficient В

Parameters of the response function

= storage discharge constant of the upper zone \mathbb{K}°

 K_{τ}

 K_{2} " " lower

= limit for slow drainage of the upper zone

Cperc = percolation capacity into the lower zone

= part of the lower zone representing lakes

and other wet areas

= maximum base in the transformation function

= parameter relating the base in the transformation function to the generated flow

The model parameters are shown in table 3.1. P_{corr}, P_{lapse}, T_{lapse} and P_w are set from information outside the calibration procedure (maps, experience etc.). The others are calibrated to optimum fit.

3.1 Snow routine

Whenever the air temperature (T) is below a threshold value (T_0) , all precipitation is regarded as snow and is accumulated in the snowpack.

All effects of evaporation and lacking representativeness of the gauge are put together in one empirical coefficient, the snow fall correction factor (C_{sf}) .

Thus, if T < T then

$$S_s = C_{sf} \cdot P,$$

where S = actual snow accumulation (mm),

C_{sf} = snow fall correction factor,

P = precipitation (mm),

 $T = surface air temperature (<math>^{\circ}C$).

Snowmelt is taken care of by the degree-day method:

If $T > T_0$, then

$$M = C_{o} (T - T_{o}),$$

where M = snowmelt (mm/day),

 $C_0 = \text{degree-day factor } (\text{mm/}(^{\circ}\text{C day})).$

The water retention in the snowpack is described by two parameters.

 C_{wh} = waterholding capacity of the snow (% of the snowpack),

S_b = bottom storage under the snow (mm).

S, has rarely been used and was therefore omitted in this work.

Refreezing of liquid water in the snowpack:

If $T < T_0$ and if there is liquid water present in the snowpack, then

$$M = C_{rfr} \cdot C_{o} (T - T_{o}),$$

where -M = refreezing rate (mm/day),

C_{rfr} = refreezing coefficient.

The area-elevation distribution of the snowroutine in the HBV-model is described by Bergström (1976). It contains no free parameters and is therefore not very interesting for the calibration of the model.

3.2 Soil moisture routine

The behaviour of the soil moisture zone is illustrated in fig. 3.2.

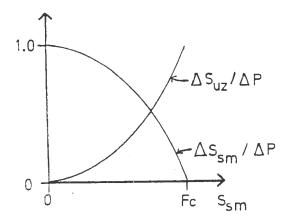


Fig. 3.2 The contributions from rainfall or snowmelt, P, to the soil moisture zone, S_{sm} , and the upper zone, S_{uz} .

Mathematically, this can be described by the following equations:

$$\frac{\Delta}{\Delta} \frac{S_{uz}}{P} = \left(\frac{S_{sm}}{Fc}\right)^{\beta}$$

$$\frac{\Delta}{\Delta} \frac{S_{sm}}{P} = 1 - \left(\frac{S_{sm}}{Fc}\right)^{\beta}$$

where P = precipitation or snowmelt (mm),

 $S_{nz} = storage in the upper zone (mm),$

 $S_{sm} = computed soil moisture storage (mm),$

Fc = maximum soil moisture storage in the model (mm),

 β = empirical coefficient,

 $_{\Delta}$ $_{\text{UZ}}^{\text{S}}$ = amount that passes through the soil moisture zone (mm),

 Δ S $_{\rm SM}$ = amount that is stored in the soil moisture zone (mm),

Δ p = precipitation or snowmelt fed into the zone mm by mm.

Potential evaporation is reduced to actual values by the function in fig. 3.3.

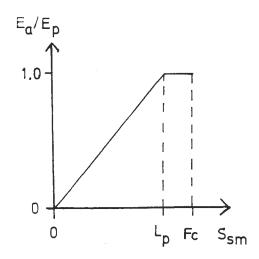


Fig. 3.3 Reduction of potential evaporation, E_p , to actual, E_a .

Mathematically described by:

$$E_{a} = \begin{cases} E_{p} & \text{if } S_{sm} \geq L_{p} \\ E_{p} & \frac{S_{sm}}{L_{p}} & \text{if } S_{sm} \leq L_{p}, \end{cases}$$

where E_p = potential evaporation,

 $E_a = actual evaporation,$

 L_{p} = limit for potential evaporation.

3.3 Response function

Having passed the soil moisture routine the excess water passes through some reservoirs, where the runoff Q_g is easily calculated in the manner illustrated in fig. 3.4.

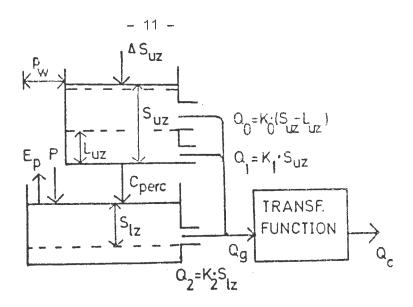


Fig. 3.4 The response function of the HBV-model.

```
= percolation capacity,
       = potential evaporation,
Ko
      = storage discharge parameter of the upper zone,
      = slow drainage storage discharge parameter of the
         upper zone,
      = storage discharge parameter of the lower zone,
K_2
      = limit for slow drainage of the upper zone,
\mathbb{P}
      = precipitation,
P_{\mathbf{w}}
      = part of the lower zone, representing wet areas,
      = total generated runoff,
Q<sub>o</sub>
      = runoff generated from the upper zone,
      = slow drainage runoff generated from the upper zone,
Q<sub>1</sub>
      = runoff generated from the lower zone
      = total computed runoff,
      = storage in the lower zone of the model,
                     " upper
      = inflow in the upper zone.
```

The transforming function multiplies Q_g with a weight differing in time. Q_g is transformed into Q_c according to fig. 3.5.

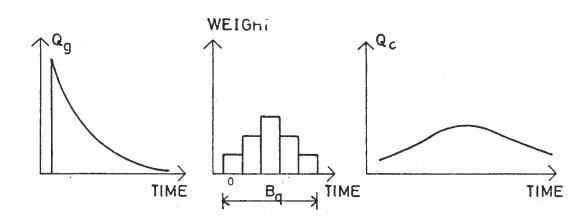


Fig. 3.5 The effect of the transformation function on the generated hydrograph.

This can be expressed as:

$$B_{q} = \begin{cases} B_{\text{max}} - C_{\text{route}} \cdot Q_{g} & \text{if } (B_{\text{max}} - C_{\text{route}} \cdot Q_{g}) \ge 1 \\ 1 & \text{if } (B_{\text{max}} - C_{\text{route}} \cdot Q_{g}) < 1 \end{cases}$$

B = base of the triangular function (days),

B = maximum base (days),

 $C_{\text{route}} = \text{free parameter } (\text{days}/(\text{m}^3/\text{s})),$

 Q_g = generated runoff from the reservoirs (m^3/s) ,

Time = 0: the day on which Q_g is generated (days).

4. STATISTICAL ANALYSIS OF THE RESIDUALS OF THE HEV-MODEL

4.1 Mechanism separation criterion (MSC)

A study of the hydrographs showed that different physical processes produced different discharge patterns. Subsequently a study of the residuals showed a similar mixture of different curve types with different statistical properties.

Chiefly three different processes were assumed.

- 1. Snowmelt
- 2. Rainfall or recession succeding rainfall or snowmelt (referred to as γ -flow)
- Dry summer- or winter-recession (referred to as low flow).

The problem was to find a good criterion to separate the days in order to obtain classes of days with approximately station—ary residuals. One method is to divide the calibration period by visual inspection. The drawbacks of this method are its subjective character and the fact that it does not take the different model mechanisms into account.

The method was therefore abandoned and the following mechaism separation criterion (MSC) was used.

2.
$$M \leq 0$$
 and $(\Delta S_{uz} > 0 \text{ or } S_{uz} > 0)$: γ -flow

3.
$$M \le 0$$
 and $(\Delta S_{uz} = 0)$ and $S_{uz} = 0$: low flow,

where M = snowmelt (mm),

 S_{uz} = storage in the upper zone of the model (mm),

 ΔS_{UZ} = inflow in the upper zone of the model (mm).

This MSC has two major drawbacks:

1. It will give different partitions of the calibration period at different parameter settings. This will disturb the behaviour of the properties studied.

2. It may be difficult to apply to other models.

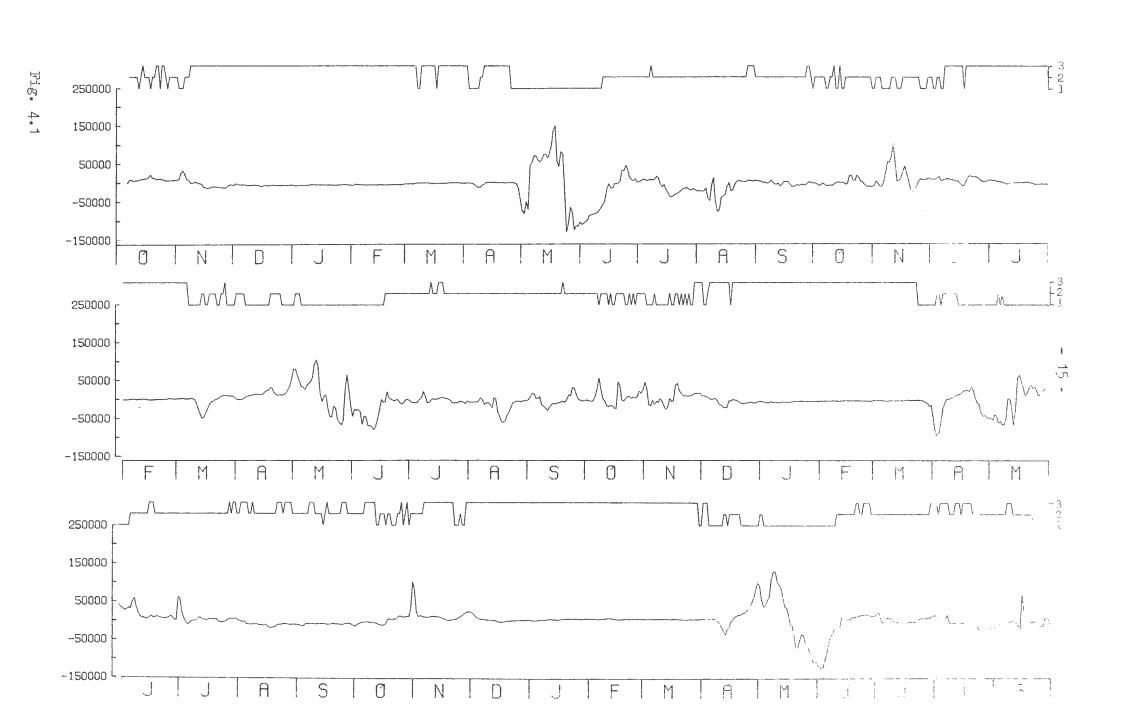
The main advantage of the chosen MSC is that it is easy to extract from the model. An example of the use of the MSC is shown in fig. 4.1.

In Kultsjön the transforming function causes a time lag, which has a maximum length of one day ($B_{max} = 2$, $C_{route} = 0.00103$, chapter 3.3). This small influence is neglected in the mechanism separation.

In Stadarforsen the time lag is much greater ($B_{max} = 6$, $C_{route} = 0$, chapter 3.3). Here the main part of the generated runoff is delayed by three days. In consequence of this the MSC was displaced three days.

Fig. 4.1 (See next page.) Residuals (1/s) and MSC of Stadarforsen 65.10.01 - 69.09.30.

- 1. Snowmelt
- Rain or recession succeeding rain or snowmelt.
- 3. Dry summer- or winter-recession.
 The upper curves show the MSC, the lower curves show the residuals.



4.2 Estimation of the density function

Mean and standard deviation of the residuals were estimated by:

$$\overline{X} = \frac{1}{n} \sum_{i=0}^{n} \left[Q_{r}(i) - Q_{c}(i) \right]$$

$$S^{2} = \frac{1}{n-1} \sum_{i=0}^{n} \left[Q_{r}(i) - Q_{c}(i) - \overline{X} \right]^{2}$$

where \overline{X} = mean value of the chosen residuals (m^3/s) ,

n = number of the chosen residuals,

 $Q_{r}(i) = observed discharge (m³/s),$

 $Q_{c}(i) = computed discharge (m³/s),$

S = standard deviation of the chosen residuals (m^3/s) .

A symmetrical interval, four standard deviations long, was placed around the mean value. The interval $(\overline{X} - 2S, \overline{X} + 2S)$ was divided into 40 equally long classes, and the number of residuals in each class was plotted in a histogram. For comparison a Normal probability distribution function with \overline{X} mean and S standard deviation was plotted in the same diagram.

As the interval of four standard deviations is too short to contain all the residuals, the number of exceeding residuals (NER) is printed together with each histogram. An example of a histogram can be seen in fig. 4.2.

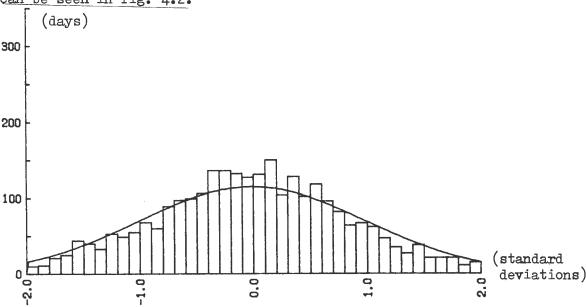


Fig. 4.2 Histogram of the low flow residuals of Kultsjön 62.10.01 – -76.05.18. Meanvalue = 0.725 (m³/s). Standard deviation = -7.07 (m³/s).

All histograms are presented in Appendix A.

A preliminary test was made to study if the mean value of each class of residuals (\overline{X}) differed dignificantly from zero. The simple t-test was used for this purpose. Some apparently significant results were found.

However, the t-test is based on the assumption of independent and $N(\mu,\sigma)$ -distributed variables. The assumption of normality is not very critical, but the assumption of independence has to be fullfilled.

As will be shown later, the residuals are not independent. The test was carried out with regard paid to the interdependence, according to Hansen (1971). Thus the quantity $\frac{n}{2 n}$ was interpreted as the equivalent number of independent observations.

Where $n_{_{_{\mathbf{v}}}}$ is defined by:

$$n_{x} = \int_{0}^{\infty} R(\tau) d\tau$$

 $R(\tau)$ = autocorrelation function of the chosen residuals.

Using the t-test in this way showed no significant deviation from zero on the 5 % level.

However, each class of residuals consists of a number of independent continuous time periods. Regarding this, one could
construct a more powerful test.

4.3 Test of normality and independence

Very often in statistical applications the assumptions of mutually independent and normally distributed variables are made.

To test these assumptions on the residuals of different model mechanisms the $\chi^2\!-\!{\rm test}$ was used.

$$U = \sum_{i=1}^{k} \frac{(Y_i - np_i)^2}{np_i}$$

where U = test variable,

k = number of test classes,

n = total number of recorded days,

p_i = probability for a normally distributed, stochastic variable
 to assume a value within class i,

Y; = observed number of days in class i.

If the assumptions hold, then U is approximately χ^2 -distributed with the number of test classes minus three degrees of freedom.

Whenever np_i < 5, the test class, i, was merged with a neighbouring test class, until the probability to fall within test class limits was greater than 5/n. This validity limit is taken from Rudemo, Råde (1970).

Let:
$$X(t) = Q_r(t) - Q_c(t)$$
, where $Q_r(t) = observed discharge at day t, $Q_c(t) = computed$ " " " ".$

Table 4.1 χ^2 -test made on the residuals. The hypothesis H_O (the X(t):s are mutually uncorrelated with Normal probability distribution function) is tested versus its logical opposite.

| Catchment | MSC | Number of observations | Degrees of freedom | Test vari- able (U) | 0.1 % level significance limit of U |
|--------------|----------|------------------------|--------------------|------------------------|-------------------------------------|
| Kultsjön | _ | 4977 | 38 | 2210 | 73 |
| ** | snowmelt | 1185 | 11 | 322 | 77 |
| ŤŤ | γ−flow | 914 | 11 | 166 | ř i |
| 11 | low flow | 2876 | 71 | 99 | FT |
| Stadarforsen | - | 5273 | 11 | 4459 | ff |
| 11 | snowmelt | 1156 | 11 | 403 | 11 |
| 11 | γ−flow | 2008 | 11 | 420 | 11 |
| 11 | low flow | 2097 | ,11 | 354 | t t |

The hypothesis (H_0) that the residuals (X(t):s) are mutually independent with Normal probability distribution function was tested by means of the χ^2 -test (tab. 4.1).

The hypothesis had to be rejected on the 0.1 % level.

Although the material was divided into different classes, the hypothesis H_{O} still did not hold. However, the χ^2 -variable (U) was made less by the separation of the different mechanisms. A visual inspection also shows that the residuals are more close to normality in each subclass after the separation. Therefore H_{O} is, in some sense, more valid after the mechanism separation of the material than before.

Furthermore, the χ^2 -test is very sensitive when used on a material built upon many observations. The data may be sufficient in number to show their inconsistency with almost any hypothesis suggested. (Hamon and Hannan, 1963).

The χ^2 -test is unfortunately not able to separate the questions of distribution and autocorrelation. As will be shown later, a clearly significant autocorrelation exists in this case. Moreover, mostly the assumption of normally distributed residuals is not very ciritical. Every result below, obtained by relying upon Normal distributions may be considered as an approximation.

4.4 Estimation of the autocorrelation

To estimate the autocorrelation a method described by Jenkins and Watts (1969) was used.

At first the autocovariance was estimated for each continuous period j, when one mechanism was working (see chapter 4.1).

$$\hat{R}_{j}(\tau) = \frac{1}{N_{j}} - \tau \qquad \sum_{t=t_{j}}^{N_{j}-\tau+t_{j}-1} (X(t+\tau) - \overline{X})(X(t) - \overline{X}),$$

where $\hat{R}_{j}(\tau)$ = estimated autocovariance of residuals separated by τ days.

 $X(t) = Q_r(t) - Q_c(t) = residual at time t (m³/s),$

 N_{j} = duration of period j (days),

t = the time at which period j started (days from the beginning of the discharge record).

In order to get an overall estimate of the autocovariance the estimates from the different periods with the same mechanism working were brought together as follows.

$$\hat{R}(\tau) = \sum_{\substack{\text{all } \\ \text{the} \\ \text{periods } j}} \frac{\binom{N_j - \tau}{T}}{\tau} \hat{R}_j(\tau))$$

where $\hat{R}(\tau)$ = overall estimate of the autocovariance,

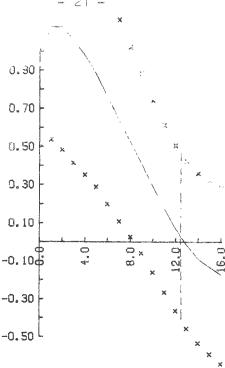
$$\mathbb{N}_{\tau} = \Sigma(\mathbb{N}_{j} - \tau) = \text{the total number of observations of } \mathbb{R}(\tau) \text{ (days).}$$

Finally the autocorrelation was estimated by dividing the estimates of the autocovariance by the estimate of the variance.

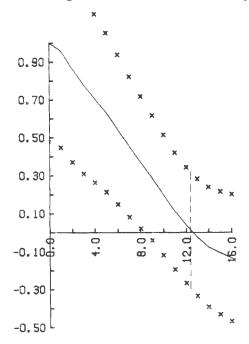
When there is less than about 400 observations, one should not rely too much upon the autocorrelation curves, because of the extremely skew probability distribution of the autocovariance.

Kendall and Stuart (1967) actually warned for the use of a correlation coefficient estimate, based on less than 500 observations. However, here we have got autocorrelation estimates at surrounding time intervals too, which gives an indication of the roughness of the estimation procedure. Furthermore the coefficients were estimated from a number of series differing in time.

During series of days with rapidly changing MSC the discharge produced by different physical mechanisms strongly interacts. This may disturb the estimation of the autocorrelation function. (See fig. 4.3, where the estimated autocorrelation exceeds 1.) To avoid this phenomenon a minimum period duration of 5 days was defined. It had to be exceeded without any change in the MSC, if the period was to be used in the autocorrelation estimation procedure. (See fig. 4.4.)



Estimate of the autocorrelation of the model residu-Fig. 4.3 als at snowmelt in Stadarforsen 61.10.01 - 76.03.31. Variance of the residuals = $1.72 \cdot 10^3 \, (\text{m}^3/\text{s})^2$. 95 % confidence limits: × >400 observations to the left of the line: Minimum period duration = 1 day.



Estimate of the autocorrelation of the model residuals at snowmelt in Stadarforsen 61.10.01 $\frac{1}{2}$ 76.03.31. Variance of the residuals = 2.35 \cdot 10³ (m³/s)². 95 % confidence limits: × > 400 observations to the left of the line: ! Minimum period duration = 5 days.

4.5 Significance of the autocorrelation

It was considered an important task to determine confidence intervals around the autocorrelation function and especially to tell when it significantly differed from zero.

One method to approach this problem is a significance test developed by Anderson (1941).

The hypothesis that the series is a so called circular series built upon N purely random observations of a normally distributed stochastic variable, is tested. This method was not used because of the difficulty of merging the different significance limits from separate time series, differing in length into an overall significance limit.

Assuming that the residuals are normally distributed and that the estimated mean value is correct, we will obtain:

$$\operatorname{Var}\left[\hat{R}_{j}(\tau)\right] = \frac{1}{N} \int_{j}^{N_{j}-\tau-1} v = -N_{j}+\tau+1 \left[R_{j}^{2}(v) + R_{j}(v+\tau) R_{j}(v-\tau)\right] \left(1 - \frac{\tau+|v|}{N_{j}}\right)$$

where $\hat{R}_{j}(\tau)$ = estimate of the autocovariance function of period j, N_{j} = duration of period j (days).

This method is described by Hjorth (1976). Assuming the $R_j(\tau)$ of different periods j with the same mechanism working as independent, we get

$$\operatorname{Var}\left[\hat{R}(\tau)\right] = \sum_{\substack{\text{all} \\ N_{\tau}}} \left(\frac{N_{j} - \tau}{N_{\tau}}\right)^{2} \cdot \operatorname{Var}\left[\hat{R}_{j}(\tau)\right]$$
periods j

Confidence intervals were computed, assuming the $\hat{R}(\tau)$:s to have normal probability distributions. Then the 95 % confidence interval was given in the form:

$$\hat{R}(\tau) \stackrel{+}{-} 1.96 \cdot \sqrt{\text{Var} \left[\hat{R}(\tau)\right]}$$

When plotted in the autocorrelation graphs all confidence limits had to be divided by $\hat{R}(o)$ in order to get the correct scale. The prodedure led to a slight paradox, the upper confidence limit might exceed one. This is of course impossible, but the autocor-

relation graph should be interpreted as a standardized autocovariance graph. The confidence limits were symmetrically placed on both sides of the autocorrelation estimate.

4.6 Analysis of the autocorrelation

During the beginning of the statistical study the autocorrelation coefficients were believed to contain valuable information.

The kind of intermittent processes described here are not known to be fitted with any standard estimation methods. An aim of this work has been to get unbiased estimations. With increasing number of observations the observed quantity turns more and more normal, and then an unbiased estimation is preferable.

The three MSC are:

```
1. M > 0 (snowmelt), 

2. M \leq 0 and (S_{uz} or \Delta S_{uz}) > 0 (\gamma-flow), 

3. M \leq 0 and S_{uz} = \Delta S_{uz} = 0 (low flow). 

M = snowmelt (mm), 

S_{uz} = storage in the upper zone of the model (mm), 

\Delta S_{uz} = inflow in the " " " " " " " ".
```

During snowmelt we have got a clearly significant autocorrelation (see fig. 4.5 and 4.6). This shows us that a large residual during one day will give rise to large residuals during the following days. If, for instance, bad representativeness of the temperature measurements causes false snowmelt one day, the reservoirs of the model are filled up to an improper level. This affects the residuals during the following days.

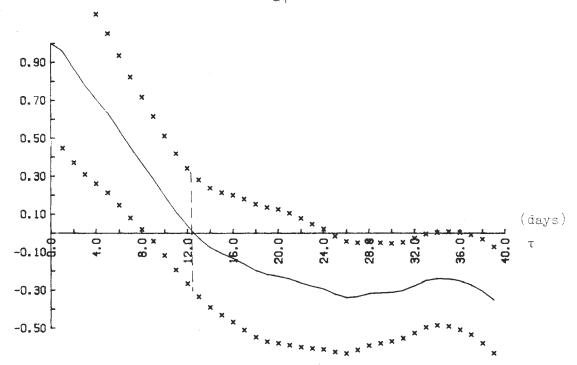


Fig. 4.5 Estimate of the autocorrelation of the residuals of Stadarforsen (snowmelt) 61.10.01 - 76.03.31.

Variance of the residuals = 2.35 · 10³ (m³/s)².

95 % confidence limits: ×

> 400 observations to the left of the line:

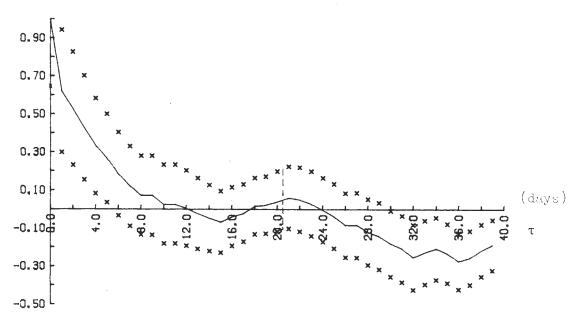


Fig. 4.6 Estimate of the autocorrelation of the residuals of Kultsjön (snowmelt) 62.10.01 - 76.05.18.

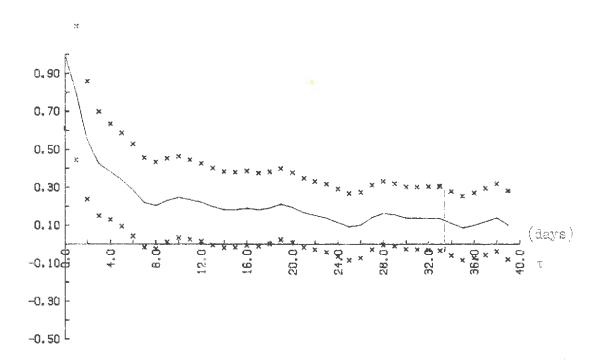
Variance of the residuals = 1.13 · 10³ (m³/s)².

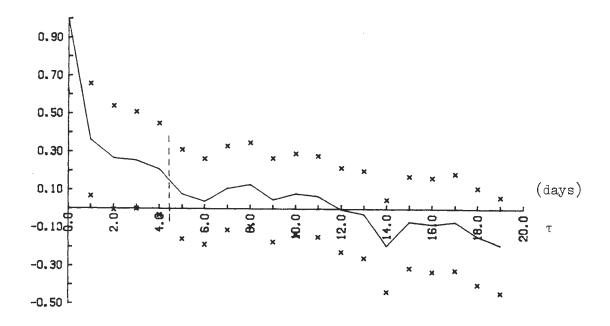
95 % confidence limits: ×

> 400 observations to the left of the line:

The simplecrease of the autologyelation undetion of States forsed compared with the one of Kultsjon is presumably due to the facts that:

- 1. The response in Stadarforsen is more tamped.
- 2. The discharge data of Stadarforser do not contain the kind of noise that lies on top of the discharge record in Kultsjön, due to the method (Bergström 1976) used when estimating inflow.





When the MSC shows γ -flow (fig. 4.7 and 4.8), we have also got a significant autocorrelation. However, it is less than in the former case. A reasonable explanation to this is that the reservoirs may still become filled up to an improper level but not up to the same high level as during snowmelt. This makes the residuals, separated by a shorter time period, independent of each other.

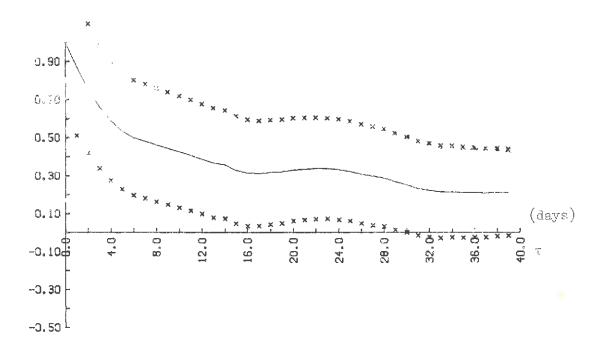


Fig. 4.9 Estimate of the autocorrelation of the residuals of Stadarforsen (low flow) 61.10.01 - 76.03.31.

Variance of the residuals = 19.3 (m³/s)².

95 % confidence limits: ×

> 400 observations everywhere.

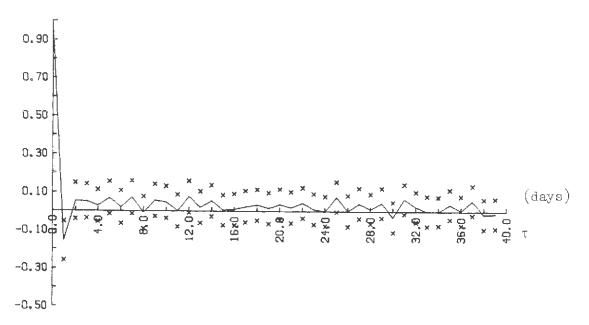


Fig. 4.10 Estimate of the autocorrelation of the residuals of Kultsjön (low flow) 62.10.01 - 76.05.18.

Variance of the residuals = 47.1 · (m³/s)²

95 % confidence limits: ×

> 400 observations everywhere.

At low flow there are great differences between Stadarforsen and Kultsjön (fig. 4.9 and 4.10).

The noise of the hydrograph of Kultsjön leads to the assumption that any autocorrelation in Kultsjön during low flow is masked by the noise on top of the recorded hydrograph.

In Stadarforsen this is not the case. A nice smooth recession curve gives us large autocorrelation estimations.

If the reservoirs of the model are filled up to an improper level during or before the winter recession, this will cause a very persistant series of residuals.

5. A STUDY OF RESPONSE SURFACES OF CRITERIA OF FIT

5.1 Criteria of fit

Nash and Sutcliffe (1970) defined the R²-criterion of fit as the efficiency of the model.

$$\mathbb{R}^{2} = \frac{\sum_{\mathbf{t}} (Q_{\mathbf{r}}(\mathbf{t}) - \overline{Q}_{\mathbf{r}})^{2} - \sum_{\mathbf{t}} (Q_{\mathbf{r}}(\mathbf{t}) - Q_{\mathbf{c}}(\mathbf{t}))^{2}}{\sum_{\mathbf{t}} (Q_{\mathbf{r}}(\mathbf{t}) - \overline{Q}_{\mathbf{r}})^{2}}$$

where $Q_{\mathbf{r}}(t) = \text{observed discharge at time t } (m^{3}/s)$, $Q_{\mathbf{c}}(t) = \text{computed}$ " " " " " , $\overline{Q}_{\mathbf{r}} = \text{arithmetic mean of } Q_{\mathbf{r}}(t)$.

The R²-criterion of fit is widely spred and it has a relative character, which makes it attractive when comparing the fit of different models, different time periods or different catchments.

These comparisons should not be made between hydrographs that differ too much, because of the phenomenon illustrated in fig. 5.1 and 5.2, which could be due to one or both of the following explanations.

- 1. Inevitable errors of roughly constant size cause the R²+criterion to give high values when applied to hydrographs with high initial variance and vice versa.
- 2. The calibration of the model and the model itself favour fit during periods with high initial variance, and so the relative fit is bound to be worse during periods with low initial variance.

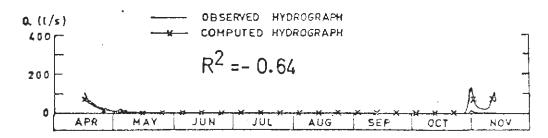


Fig. 5.1. Low R^2 -value as a result of low initial variance (Stabby, 1959). (From Bergström, 1976.)

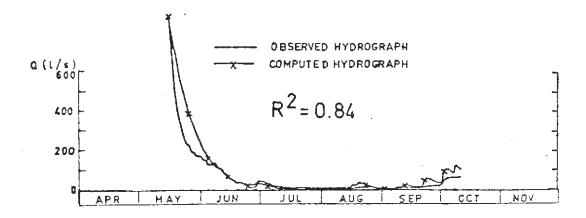


Fig. 5.2. High R²-value as a result of high initial variance (L. Tivsjön. 1968). (From Bergström, 1976.)

The initial variance from a sample of n observations is defined by:

$$F_o^2 = \frac{1}{n-1} \sum_{t=1}^n (Q_r(t) - \overline{Q}_r)^2.$$

The R²-criterion was computed for each class and also for the material as a whole. The obtained criteria are called:

 R_1^2 during snowmelt, R_2^2 during rain or recession succeeding rain or snowmelt (γ -flow), R_3^2 during dry summer or winter recession (low flow),

for the material as a whole,

$$R_{sum} = R_1^2 + R_2^2 + R_3^2$$

Up till today the R_w^2 -criterion has been used as a help during the calibration by visual inspection of the hydrograph.

Let us assume that the R^2 -criteria of different physical processes do give a more accurate measure of the goodness of fit between the computed and the recorded hydrograph. Then the problem of merging the three criteria into one arises. One possibility of doing this is simply to add up the three criteria, thus achieving the R_{sum} -criterion.

5.2 Basic assumptions and observations

The MSC gives different classifications of the material at different parameter settings. This sometimes made the R^2 -criteria vary unexpectedly (especially the R_3^2 -criterion). If a couple of days are moved to the low flow class from the other classes, this will probably make the initial variance (F_0^2) of the low flow class greater, but it might possibly not influence the sum $\frac{\Sigma}{t}(Q_{\mathbf{r}}(t)-Q_{\mathbf{c}}(t))$ to the same extent. Thus, the R_3^2 -criterion will grow perhaps without any visible change in the hydrograph, a phenomenon similar to the one illustrated in fig. 5.1 and 5.2.

The HBV-model has always been calibrated by visual inspection of the computed and recorded hydrographs. This means that a considerable skill in parameter setting has been obtained during the years. For example, recently on the first try when calibrating the HBV-model for a new catchment the $R_{\rm W}^2$ -value of the four year calibration period was greater than 0.8.

This implies that a fairly good parameter setting could be obtained by a qualified guess based on experience from other applications. It is likely that an automatic parameter optimization routine would accomplish this too.

This assumption made the work easier, while only the region around the optimum parameter setting had to be examined. The subjectively found optimum (tab. 5.1) was used as the actual one, and the parameters were varied around this central point.

Table 5.: Original settings of the free parameters of the HBV-model.

| Parameter | Kultsjön | Stadarforsen |
|--|----------|--------------|
| Pcorr | 1.330 | 1.136 |
| T _o (°C) | 0.5 | 0.0 |
| C _{sf} | 1.23 | 0.90 |
| $C_{\circ} (mm/({}^{\circ}C \cdot day))$ | 3.2 | 2.0 |
| C wh | 0.05 | 0.05 |
| S _b (mm) | 0.0 | 0.0 |
| $^{ m C}_{	extbf{rfr}}$. | 1.0 | 1.0 |
| Fc (mm) | 150 | 150 |
| $_{ m p}^{ m L}$ (mm) | 150 | 150 |
| β | 3.0 | 1.5 |
| $K_{_{\mathrm{O}}}$ (1/(s · mm)) | 0 | 12500 |
| K ₁ (1/(s · mm)) | 4000 | 3500 |
| K ₂ (1/(s · mm)) | 300 | 350 |
| Luz (mm) | ∞ | 15 |
| C _{perc} (mm/day) | 1.3 | 1.0 |
| B _{max} (days) | 2.0 | 6.0 |
| Croute (day · s/m ³) | 0.00103 | 0.00000 |

Note that $K_{\rm o}$ in Kultsjön is zero. That version of the HBV-model is older than the one used in Stadarforsen. It is occasionally used when the catchment behaviour is determined to be sufficiently simple. Because there were no initial values of $K_{\rm o}$ and $L_{\rm uz}$, a variation of these parameters in Kultsjön was avoided.

During the original subjective calibration 8-year periods were used, but due to the limited capacity of the computer only 4-year periods were used in the study of the response of the R²-criteria. This limits the value of the comparisons between the model behaviour of the original parameter setting and the test settings of this study. The periods studied are in Stadarforsen 1965-10.01-1969-09-30 and in Kultsjön 1962-10-01-1966-09-30.

Two, sometimes three, parameters were varied simultaneously, and the R²-criteria were computed at the different parameter settings. This resulted in tables and "three-dimensional" diagrams of iso-R² graphs. The R²-curves were only drawn around the optimum point.

If there was a substantial difference between the R²-values at the optimum and at the original parameter setting, the computed hydrograph corresponding to the optimum values of the parameters — was plotted. These hydrographs were later judged by the model calibraters in order to estimate the goodness of fit at the new parameter settings.

R²

| К ₂ | 100 | 200 | 300 | 400 | 500 | 600 | 700 | 800 | 900 | 1000 |
|--------------------|-------|--------|-------|------|------|------|------|------|------|------|
| C pe r c | | | | | | | | | | |
| 9 | .704 | 709 | -740 | 709 | .707 | | • | • | | • |
| 12 | •797 | .714 | .716 | .715 | -713 | | • | • | | • |
| 15 | .709 | .718 | .721- | 720 | .719 | • | • | • | • | • |
| 18 | .708 | 720 | .724 | .725 | .724 | • | | • | | |
| 21 | .706 | 720 | .727 | .728 | .728 | • | • | | • | • |
| 24 | .70/1 | .\719 | .727 | 730 | 730 | .729 | .727 | •725 | .723 | .721 |
| 27 | .694 | .715 | .727 | .731 | •732 | .731 | 730 | .728 | .726 | .724 |
| 30 | .685 | \.711\ | .725 | .731 | •733 | .733 | .732 | 730 | .728 | .726 |
| 33 | •674 | .704 | 722 | 730 | •734 | •734 | •733 | .732 | 730 | .728 |
| 36 | • | . \ | .\ | _/ | | •735 | •734 | •733 | .732 | 730 |

 R_{2}^{2}

| [™] 2 | 100 | 200 | 300 | 400 | 500 | 600 | .700 | 800 | 900 | 1000 |
|---------------------------------|---------------|--------|------|--------------|--------------|------|-------|------|-------|------|
| $^{\mathrm{C}}_{\mathtt{perc}}$ | | | | | | | | | | |
| 9 | .538 | •543 < | •538 | •530 | •522 | • | • | • | ٠ | • |
| 12 | -548 | •554 | .547 | •539 | •530 | • | • | • | | • |
| 15 | .551 | •559 | .552 | ·54× | .536 | • | • | • | | • |
| 1 8 | .555 | .566 | .558 | 550 | . 542 | • | | • | | • |
| 21 | • 5 57 | . 569 | 560 | •552 | .544 | • | • | • | • | • |
| 24 | .551 | . 566 | ·559 | .5\$1 | . 545 | 540 | • 534 | .528 | .520 | .512 |
| 27 | .552 | .567 | •558 | <u>,8</u> 51 | • 546 | ·542 | • 537 | .531 | .525 | .518 |
| 30 | •543 | .559 | •549 | -543 | 540 | •537 | •534 | .530 | .525 | .519 |
| 3 3 | .533 | •549- | -539 | •533 | •532 | •532 | .531 | •529 | . 525 | .520 |
| 36 | • | • | • | • | • | •524 | .524 | .524 | . 520 | .519 |

Fig. 5.3 The response of the R^2 -criteria to K_2 (1/(s · mm)) and $C_{\rm perc}$ (10⁻¹ mm/day) at Kultsjön. (See chapter 5.3; 5.3.1)

R²3

| к ₂ | 100 | 200 | 300 | 400 | 500 | 600 | 700 | 800 | 900 | 1000 |
|----------------|------|-------|----------|------|-------|-------|-------|-------|-------|-------|
| Cperc | | | | | | | | | | |
| 9 | .145 | . 233 | .254 | .248 | .232 | • | • | • | • | • |
| 12 | .161 | •274 | .306 | .306 | •293 | • | • | • | • | • |
| 15 | .151 | .286 | .328 | •332 | • 323 | • | • | • | • | • |
| 18 | .141 | •292 | •344 | •355 | - 351 | • | • | • | • | • |
| 21 | •113 | .285 | • \$47 (| .365 | .366 | | • | · · | • | • |
| 24 | .079 | .265 | •333 | •354 | . 358 | -354 | .347 | • 337 | .327 | .316 |
| 27 | .067 | .260 | •332(| .358 | .367 | . 368 | .364 | 358 | >350 | .341 |
| 30 | .024 | .229 | .307 | .337 | 350 | • 353 | •352 | •348 | . 341 | • 334 |
| 33 | .009 | .220 | .300 | •334 | .349 | .356 | • 358 | • 356 | .358 | •347 |
| 36 | • | • | • | • | • | .336 | •341 | • 341 | • 339 | • 335 |
| | | | | | | | | | | |

 $R_{\mathbf{w}}^{2}$

| K ₂ | 100 | 200 | 300 | 400 | 500 | 600 | 700 | 800 | 900 | 1000 |
|----------------|------|----------------------|------|-------|-------|------|-------|------|------|------|
| Cperc | | | | | | | | | | |
| 9 | •777 | .783 | .783 | .782 | .780 | • | • | • | • | • |
| 12 | .780 | .788 | .789 | .788 | .786 | • | • | • | • | • |
| 1 5 | .781 | 190 | •792 | .792 | 790 | • | • | • | • | • |
| 18 | .780 | .791 | •795 | •795 | •793 | • | • | | • | • |
| 21 | •777 | .791 | .796 | .796 | • 795 | | • | • | • | • |
| 24 | .772 | .789 | •795 | •797 | .796 | •795 | • 793 | .791 | •789 | .787 |
| 27 | .766 | .786 | •794 | .796 | •797 | .796 | • 794 | •793 | .792 | 790 |
| 3 0 | •759 | .789 .786 .781 | 791 | • 795 | .796 | .796 | • 795 | -793 | .792 | .790 |
| 33 | .751 | .776 | .787 | •792 | .794 | •795 | •795 | .794 | •792 | .791 |
| 3 6 | | • | | | | | | | | |

5.3 The response surfaces of criteria of fit and test plottings of Kultsjön

For the interpretation of the model parameters see chapter 5 and for the initial values of the parameters see tab. 5.1.

5.3.1 The response of the R^2 -criteria to K_2 and C_{perc}

The variation of each \mathbb{R}^2 -criterion was computed when altering K_2 and \mathbb{C}_{perc} . Since these parameters have their greatest influence on low flow, the \mathbb{R}^2_3 -criterion was considered most important. In fig. 5.3 the \mathbb{R}^2_3 -criterion indicates that \mathbb{C}_{perc} and \mathbb{K}_2 should be increased. The irregular shape of the \mathbb{R}^2_3 -response surface is due to the variable classification by the MSC (chapter 5.2).

An increase in ${\rm C}_{
m perc}$ will have the effect of increasing the overall flow during low flow. It will also cause a shorter duration of the peak flows. An increase in ${\rm K}_2$ will accelerate the low flow recession. A test plotting was made at:

$$K_2 = 600 \text{ l/s} \cdot \text{mm},$$
 $C_{\text{perc}} = 2.7 \text{ mm/day},$

which is the optimum point during low flow.

The new hydrograph was considered to be somewhat better than the old one.

5.3.2 The response of the R²-criteria to K₁, B_{max} and C_{route}

The R_2^2 -criterion in fig. 5.4 obviously points towards a decrease in K_1 and $C_{\rm route}$. A decrease in K_1 will make the hydrograph more damped and will also cause a considerable number of days to move from the low flow class to the Y-flow class. The latter is the reason why we get such odd information from the R_3^2 -criterion here.

 $^{\rm C}$ route, too, affects the variance of the hydrograph. A low $^{\rm C}$ route value will damp the discharge peaks, while a high value will make the hydrograph vary in a more rapid way.

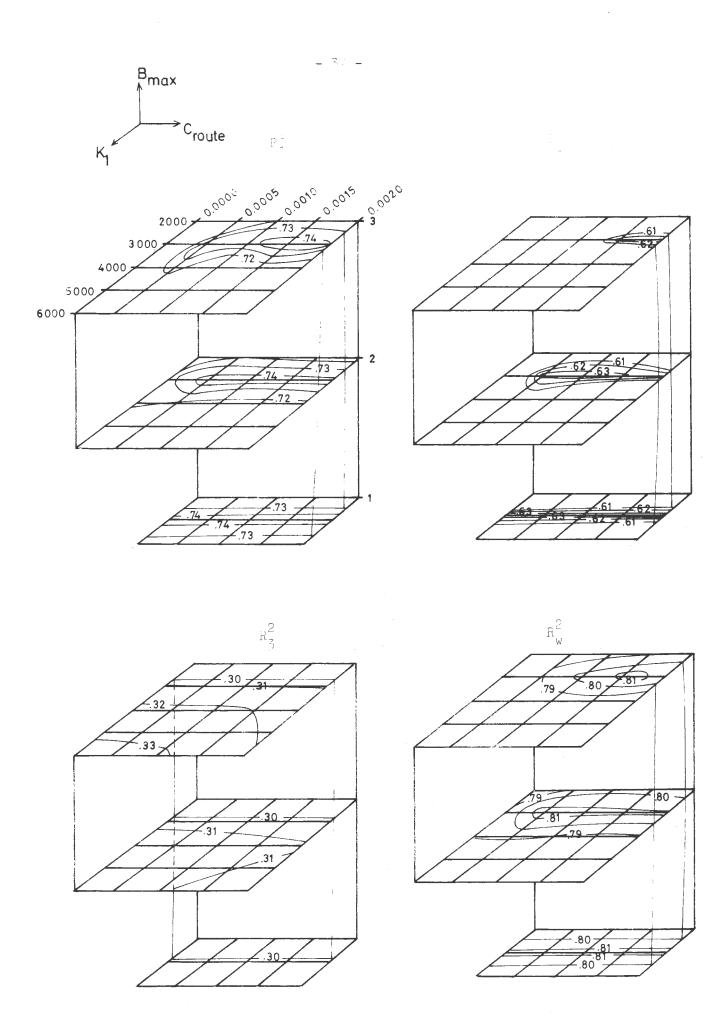


Fig. 5.4 The response of the R^2 -criteria to K_1 (1/(s · mm)), $\frac{1}{1}$ max (days) and C_{route} (day · s/m³) at Kultsjön. (See chapter 5.3; 5.3.2)

A test planting was made at:

$$E_1 = 5000 \text{ l/s} \cdot \text{mm},$$
 $C_{\text{route}} = 0.001 \text{ day/(m}^{5}/\text{s}),$
 $E_{\text{max}} = 2 \text{ days}.$

Here the model demonstrates an unability to move rapidly between high and medium flows by consistently underestimating high flows. This underestimation was considered serious and caused the calibraters to judge the plotting to be not as good as the original one.

The lack of a K_0 parameter is likely to be the cause of this damped behaviour of the model, since one further storage discharge parameter would increase the slope of the recession.

5.3.3 The response of the R^2 -criteria to Fc, L_p /Fc and β

The parameters varied in fig. 5.5 affect the evaporation. They also affect the level of the flow peaks succeeding dry periods.

The optimum of the R_W^2 -cirterion seems to be:

Fe = 200 mm,

$$L_p/Fe = 0.6 - L_p = 120 mm$$
,
 $B = 2 \text{ or } 4.$

Two test plottings are made, one at $\beta=2$ and one at $\beta=4$. They do not differ much from each other, but they differ from the original plotting. The decrease in the L_p/Fc ratio causes an increase in the evaporation. This leads to an underestimation of the high flow peaks of summer. Thus, the test plottings were inferior to the original one. The medium and low summer flows are perhaps a bit better on the test plottings than on the original one. Again the lack of a third storage discharge parameter (K_0) is obvious.

Fig. 5.5 (See next page). The response of the R^2 -criteria to Fc, L_p/Fc and β at Kultsjön.

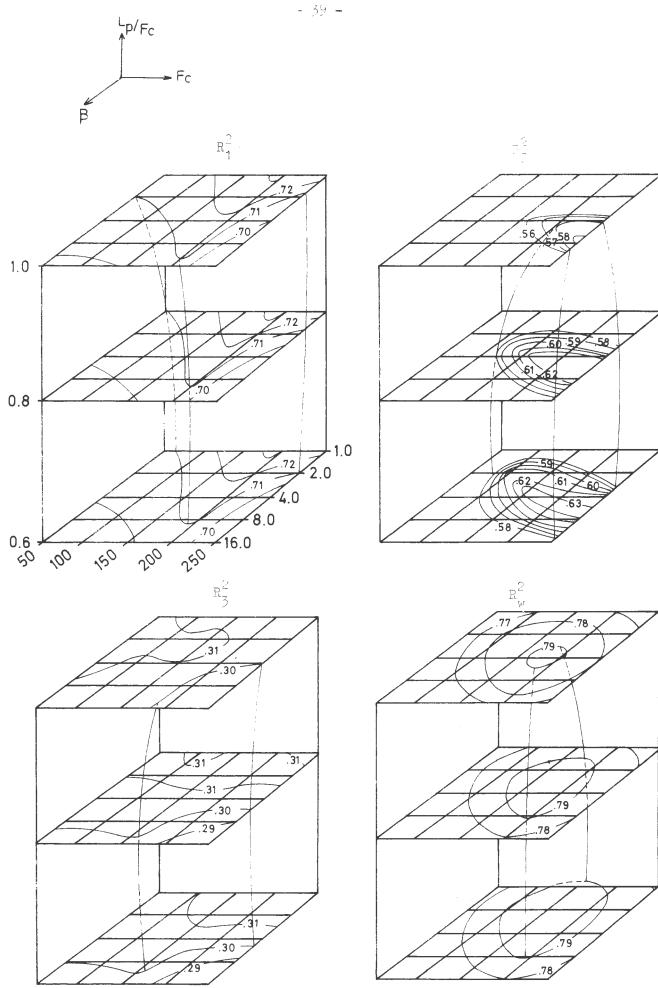


Fig. 5.5 (See chapter 5.3; 5.3.3)

5.3.4 The response of the R^2 -criteria to $C_{\underline{sf}}$ and β

 β and $C_{\rm sf}$ both affect the losses between precipitation and runoff. The differences between the optima of these response surfaces and the $R^2\text{-values}$ of the original parameter setting was small and no test plotting was made.

| | R | 2 1 | | | | | ₹ ² 3 | | | |
|----------------|------------------------------|----------------------|----------------------|-----------------|--------------|-------------------|-------------------|--------|--------------|--------------|
| c | 1. 2. | 4. | 8. | 16. | ċ | 1. | 2. | 4. | 8. | 16. |
| Csi | | | | | C sî | | | | | |
| 1.0 | .699 .69 | 0 .671 | .651 | .637 | 1.0 | •317 _\ | .323 | , •319 | •315 | . 306 |
| 7.1 | .737 .72 | 9 .715 | .700 | .689 | 1.1 | . 313 | .319 | •315 | . 309 | . 305 |
| 1.2 | -737_13 | 0 722 | | .706 | 1.2 | .308 | •315 | •312 | 310 | . 305 |
| 1.3 | .686 .68 | 0 .678 | .675 | .672 | 1.3 | . 303 | .301 | . 308 | .304 | .302 |
| 1.4 | .607 .60 | 3 .608 | .610 | .609 | 1.4 | .299 | .297 | .305 | .301/ | -299 |
| | | | | | | | | | | |
| | | 9 | | | | | 2 | | | |
| | R | 2 | | | | | R_W | | | |
| | 1. 2. | 2 4. | 8. | ¹ 6, | | 1. | R _w ? | 4. | 8. | 16. |
| o C | | | 8. | ⁴ 6, | o C sf | 1. | | | 8. | 16. |
| 0 sf 1.0 | | 4. | 8. .485 | 16. •359 | | 1. •765 | 2. | | | |
| | 1. 2. | 4. | | | Csf | | 2. | .766 | .748 | |
| 1.0 | 1. 2. | 4. | . 485 | •359 | °sf 1.0 | .765 | 2. 774 | .766 | .748 | .728 .758 |
| 1.0 | 1. 2. .396 54 .368 .53 | 4. 0,561 5,565 | .485 .501 .499 | •359 •377 | °sf 1.0 | ·765 | 2. 774 75 ā | .766 | •748 •776 | .728 .758 |

Fig. 5.6 The response of the R^2 -criteria to $C_{\rm sf}$ and β at Kultsjön.

 \mathbb{R}^2_1

| | | | | R | 1 | | | | |
|--|------------------------------|--------------------------------------|------------------------------|---|---|--|---|---|-------------------------|
| Co | 1.4 | 1.7 | 2.0 | 2.3 | 2.6 | 2.9 | 3.2 | 3∙5 | 3.8 |
| To | | | | | | | | | |
| -1.0 | .670 | .714 | .672 | .598 | | | | | ø |
| -0.5 | .612 | .709 | <u> </u> | 726 | .675 | .612 | •539 | .466 | - 3 99 |
| 0.0 | .468 | . 610 | .707 | 745 | 344 | .716 | .668 | .618 | .558 |
| 0.5 | .221 | -425 | .532 | .633 | .689 | .706 | .717 | .697 | .665 |
| 1.0 | | • | | • | •473 | •546 | .582 | .608 | .620 |
| 1.5 | | • | • | • | .211 | .251 | .307 | •357 | -395 |
| | | | | | | | | | |
| | | | | R | 2 | | | | |
| °° | 1.4 | 1.7 | 2.0 | 2.3 | 2.6 | 2.9 | 3.2 | 3-5 | 3.8 |
| T_{o} | | | | | | | | | |
| -1.0 | •513 | .482 | ·553 | .567 | . / | • | • | • | • |
| -0.5 | •449 | .478 | •492 | .551 | .556 | •555 | . 515 | •492 | • 446 |
| 0.0 | -292 | -419 | .446 | .503 | -549 | € 582 | -539 | •549 | -517 |
| 0.5 | -570 | .318 | .450 | -447 | -492 | .540 | .554 | €7T | 585 |
| 1.0 | | • | • | • | •433 | •452 | •499 | .511 | • 553 |
| 1.5 | • | | • | • | -344 | .398 | .4 08 | - 467 | •500 |
| | | | | | | | | | |
| | | | | R. | 2 | | | | |
| c _o | 1.4 | 1.7 | 2.0 | | 2 3 2.6 | 2.9 | 3.2 | 3.5 | 3.8 |
| C _o | 1.4 | 1.7 | 2.0 | | | 2.9 | 3.2 | 3.5 | 3.8 |
| T _o | 1.4 .277 | 1.7 | 2.0 .317 | | | 2.9 | 3.2 | 3.5 | 3.8 |
| T _o | | | | 2.3 | | 2.9 | • 1 | 3.5 | 3.8 |
| T _o -1.0 | .277 | .299 | .347 | 2.3 .325 | 2.6 | | • ; | | |
| T _o -1.0 -0.5 | .277 .273 .263 | .299 .285 | .317 .303 .287 | 2.3 .325, | 2.6 | . 336 | -337 | -329 | .314 |
| T _o -1.0 -0.5 0.0 | .277 .273 .263 | .299 .285 .278 | .317 .303 .287 | 2.3 .325, .320 | .332 | .336 | •337 •336 | .329 | .314 |
| T _o -1.0 -0.5 0.0 0.5 | .277 .273 .263 | .299 .285 .278 | .317 .303 .287 | 2.3 .325, .320 | | .336 .329 | • 337 • 336 • 315 • 305 | .329 .337 .321 | • 314 • 338 • 323 |
| T _o -1.0 -0.5 0.0 0.5 1.0 | .277 .273 .263 | .299 .285 .278 | .317 .303 .287 | 2.3 .325, .320 | | .336 | • 337 • 336 • 315 • 305 | .329 .337 .321 | . 314 .338 .323 |
| T _o -1.0 -0.5 0.0 0.5 1.0 | .277 .273 .263 | .299 .285 .278 | .317 .303 .287 | 325 320 302 .281 | . 332 . 346 . 292 . 286 . 274 | . 336 | • 337 • 336 • 315 • 305 | .329 .337 .321 | . 314 .338 .323 |
| T _o -1.0 -0.5 0.0 0.5 1.0 1.5 | .277 .273 .263 .243 | .299 .285 .278 .265 | .303 .287 .274 | 325 320 302 .281 | .332 .346 .292 .286 .274 | | • 337 • 336 • 313 • 305 • 285 | . 329 .337 .321 .311 | |
| T _o -1.0 -0.5 0.0 0.5 1.0 1.5 | .277 .273 .263 .243 | .299 .285 .278 .265 | .303 .287 .274 | 2.3 .325 .302 .281 | .332 .346 .292 .286 .274 | | • 337 • 336 • 313 • 305 • 285 | . 329 .337 .321 .311 | |
| T _o -1.0 -0.5 0.0 0.5 1.0 1.5 | .277 .273 .263 .243 | .299 .285 .278 .265 | .303 .287 .274 | 2.3 .325, .302 .281 | .332 .346 .292 .286 .274 R _W ² | | • 337 • 336 • 313 • 305 • 285 | .329 .337 .321 .288 | |
| T _o -1.0 -0.5 0.0 0.5 1.0 1.5 | .277 .273 .263 .243 | .299 .285 .278 .265 | .317 .303 .287 .274 | 2.3 .325, .302 .281 | 2.6 .332 .292 .286 .274 R _W ² 2.6 | 336 .329 .390 .292 .282 | -337 -336 -313 -305 -285 | .329 .337 .321 .288 | |
| T _o -1.0 -0.5 0.0 0.5 1.0 1.5 | .277 .273 .263 .243 | .299 .285 .278 .265 | .317 .393 .287 .274 . | 2.3 .325, .320 .302 .281 | 2.6 .332 .292 .286 .274 R _W ² 2.6 | 336 .329 .390 .292 .282 | -337 -336 -315 -305 -285 | . 329 .337 .321 .288 3.5 | |
| T _o -1.0 -0.5 0.0 0.5 1.0 1.5 | .277 .273 .263 .243 | .299 .285 .278 .265 .765 | .317 .393 .287 .274 | 2.3 .325 .320 .302 .281 .704 | 2.6 .332 .346 .292 .286 .274 R _W ² 2.6 | 336 .329 .380 .292 .282 2.9 | .337 .336 .313 .305 .285 | .329 .337 .321 .288 3.5 .620 | |

Fig. 5.7 The response of the R²-criteria to T and C (mm/(°C · day)) at Kultsjön. (See chapter 5.3; 5.3.5)

5.3.5 The response of the R²-criteria to T and C

 T_{o} affects the starts of the melt periods, while C_{o} affects the overall melt ratio (fig. 5.7).

A test plotting was made at:

$$T_0 = 0.0 \, ^{\circ}C,$$
 $C_0 = 2.6 \, \text{mm/(}^{\circ}C \, ^{\circ} \, \text{day)}.$

The test plotting showed out to be inferior to the original plotting. There seems to be no way to make the model fit the recorded hydrograph on both peak flow and medium flow. One further degree of freedom is needed.

5.3.6 The response of the R^2 -criteria to $C_{\rm wh}$ and $C_{\rm rfr}$

The parameters $C_{\rm wh}$ and $C_{\rm rfr}$ influence the behaviour of the model, when a melt period is restarted after a short interruption by too low temperatures. The use of the $C_{\rm rfr}$ parameter started during this study of the HBV-model, and the value of having such a parameter was questioned.

As the response surfaces (fig. 5.8) show, $C_{\rm rfr}$ does not affect the R^2 -criteria very much, so the $C_{\rm rfr}$ parameter seems to be of no use here.

The optimum value of C_{wh} is obviously 0.05. No test plotting was made, since the optimum values of C_{wh} and C_{rfr} do not deviate from the original ones.

$$R_1^2$$

Crfr 0.00 0.65 0.10 0.20 0.40 1.6
Cwh
0.00 .701 .701 .701 .701 .701 .
0.05 .709 .704 .708 .715 .715 .717
0.10 .714 .686 .602 .684 .677 .
0.15 .709 .665 .660 .661 .644 .
0.20 .700 .635 .630 .628 .604 .

R_2^2

 Crfr
 0.00
 0.05
 0.10
 0.20
 0.40
 1.00

 Cwh
 0.00
 .566
 .566
 .566
 .566
 .566
 .566
 .566
 .551

 0.05
 .564
 .561
 .557
 .553
 .550
 .

 0.10
 .562
 .555
 .551
 .547
 .543
 .

 0.20
 .556
 .547
 .543
 .540
 .534
 .

R_3^2

Crfr 0.00 0.05 0.10 0.20 0.40 1.00 Cwh 0.00 .326 .326 .326 .326 .326 .326 .326 .00.05 0.10 0.20 0.40 1.00 0.00 Cwh 0.00 0.326 .326 .326 .326 .326 .326 .00.05 .328 .318 .317 .315 .314 .313 0.10 .323 .306 300 .298 .295 .00.15 .320 .292 .289 .286 .286 .00.20 .313 .287 .284 .283 .281 .

\mathbb{R}_w^2

Crfr 0.00 0.05 0.10 0.20 0.40 1.00 Cwh 0.00 .770 .770 .770 .770 .770 .005 .778 .783 .785 .787 .789 .790 0.10 .784 .781 .780 .781 .778 .015 .785 .773 .771 .772 .765 .020 .783 .761 .760 .759 .748 .

Fig. 5.8 The response of the n^2 -criteria to $0_{\rm wi}$ and $0_{\rm rir}$ at Multsjön. (See c)apter 5.3; 5.3.6)

F.3

| E. | 10% | 100 | Ju' · | 400 | 500 |
|-------------------|------|-------|-------|------|------|
| C _{rero} | | | | | |
| 0.0 | ,04c | .866 | .207 | .868 | .869 |
| 0.5 | .886 | .886 | 7.886 | | .986 |
| 1.0 | .893 | .895 | .896 | .895 | .895 |
| 1.5 | 183. | .893 | .894 | .894 | .894 |
| 2.0 | .864 | .877- | 380 | .881 | .881 |

| | | R_2^2 |) - | | |
|-------|--------------|---------|--------|------|------|
| к2 | 100 | 200 | 300 | 400 | 500 |
| Cperc | | | | | |
| 0.0 | .571 | .576 | •577 | •574 | .568 |
| 0.5 | .693 | .706 | .711 | .711 | .706 |
| 1.0 | .677 | .734 | (751 | .756 | 755 |
| 1.5 | .623 | .717 | .747 | .758 | .759 |
| 2.0 | .5 60 | .676 | .713 | .726 | .727 |

| | | R | 2 | | |
|----------------|--------|------|------|-------|------|
| K ₂ | 100 | 200 | 300 | 400 | 500 |
| Cperc | | | | | |
| 0.0 | .000 | .000 | .000 | .000 | .000 |
| 0.5 | -1.470 | 381 | 301 | 495 | 774 |
| 1.0 | 227 | .468 | 649 | 636 | .530 |
| 1.5 | 101 | •332 | .500 | •545 | .521 |
| 2.0 | 043 | .228 | .365 | • 423 | .431 |

| | | R | 2 w | | |
|----------------|-------|------|--------|------|-------------------|
| K ₂ | 100 | 200 | 300 | 400 | 500 |
| Cperc | | | | | |
| 0.0 | .872 | .873 | .874 | .874 | .874 |
| 0.5 | .702 | .905 | - 905 | .905 | . 904 |
| 1.0 | .905/ | .914 | -917 | .917 | •9 1 6 |
| 1.5 | .325 | -210 | .914 | •915 | .914 |
| 2.0 | .872 | .892 | 898_ | 900 | .901 |

Fig. 5.: The response of the l^2 -criteria to E_2 (l_2 (s.* Lm)) and l_2 perc (in day) at Stanarforse . (See chapter 5.4; 5.4.1)

5.4 The response surfaces of criteria of fit and test plottings of Stadarforsen

In Stadarforsen runoff data of better quality than in Kultsjön were available. For the interpretation of the model parameters see chapter 3 and for the initial values of the parameters see tab. 5.1.

5.4.1 The response of the R²-criteria to K and C perc

There is no difference between the optimum parameter setting here (fig. 5.9) and the original one, and so no test plotting was made.

There has been difficulties in finding the optimum setting of K_2 and $C_{\mathtt{perc}}$. But note that there is a clearly observable optimum in the dry summer and winter recession class here.

The original parameter setting is within the limits of acceptance in fig. 5.10. The $R_{\rm w}^2$ -criterion does not vary much when B is varied in a region around the original parameter setting. To study this apparent independence a test plotting was made at:

$$K_1 = 3500 l/s \cdot mm,$$
 $C_{\text{route}} = 0 \text{ day/(m}^3/s),$
 $B_{\text{max}} = 5 \text{ days,}$

where there is a small improvement of the $R_{\rm w}^2$ -criterion but the new plotting had approximately the same fit as the original one, as judged by the calibrators.

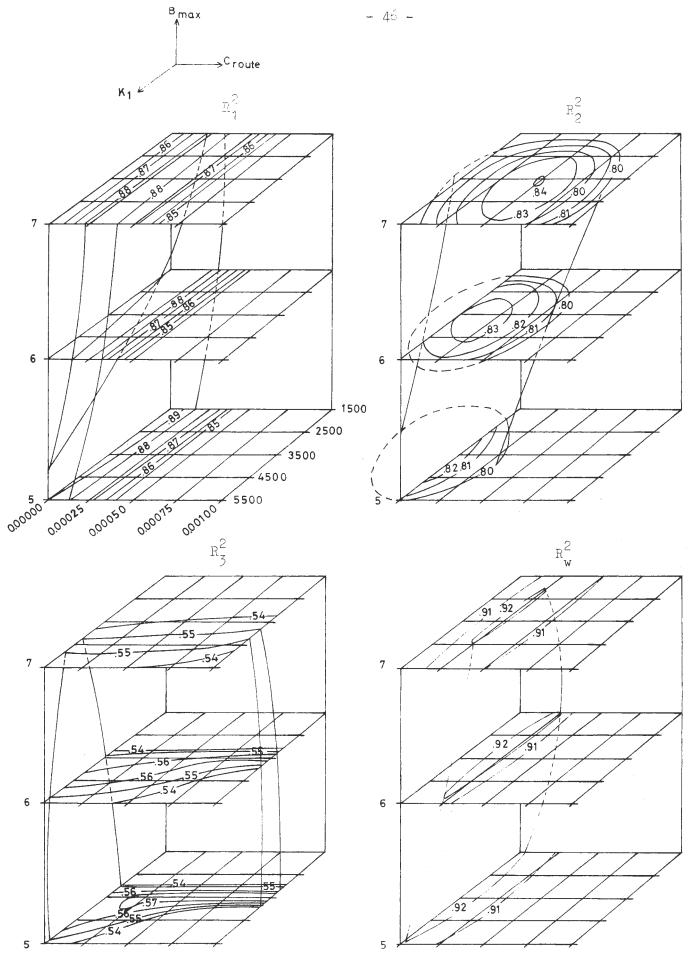


Fig. 5.10 The response of the R²-criteria to K₁ (1/(s · mm)), C_{route} (day · s/m³) and \mathbb{B}_{\max} (days) at Stadarforsen. (See chapter 5.4; 5.4.2)

| | | | | H2 | | | | |
|----------------|---------------|-------|--------|--------------------|-------|-------|------------------|----------|
| K o | 7500 | 10000 | 12500 | 15000 | 17500 | 25000 | 235,00 | 25000 |
| Luz | | | | | | | | |
| 5 | .796 | .850 | .870 | .875 | .870 | | | |
| 10 | -794 | .851 | .875 | .884 | .805- | | • | • |
| 15 | .790 | .850 | .679 | .891 | .894 | - | • | • |
| 20 | .783 | .846 | .878 (| .894 | .901 | -901_ | .899 | .894 |
| 25 | •774 | .838 | .873 | 892 | 1.901 | .905 | .905 | .903 |
| 30 | • | | . \ | .\ | , | .903 | .906 | .906 |
| | | | | | | | | |
| | | | | R_2^2 | | | | |
| Ko | 7500 | 10000 | 12500 | 15000 | 17500 | 20000 | 22500 | 25000 |
| $^{ m L}$ uz | | | | | | | | |
| 5 | •794 | .752 | .692 | .628 | .567 | • | • | • |
| 10 | .819 | .809 | .782 | •753 | .721 | • | • | • |
| 15 | .828 | .836 | 831 | .819 | .806 | • | • | • |
| 20 | .820 | .841 | .847 | .848 | 846 | -842 | .837 | 832 |
| 25 | .798 | .824 | -837 | .845 | 850 | .853 | .655 | 856 - |
| 30 | • | • | | | - | .833 | 837 - | .841 |
| | | | | _ | | | | |
| | | | | R ² | | | | |
| Ko | 7500 | 10000 | 12500 | 15000 | 17500 | 20000 | 22500 | 25000 |
| Luz | | | | | | | | |
| 5 | .566 | •537 | .508 | .487 | • 453 | • | • | • |
| 10 | .551 | •543 | -544 | -533 | .524 | • | , | • |
| 15 | .511 | 543 | •550 | •549 | -549 | • | • | • |
| 20 | .4 96 | •504 | • 505 | •505 | .512 | •514 | •518 | •519 |
| 25 | . 4 83 | •492 | .496 | • 496 | . 496 | .504 | • 504 | •504 |
| 30 | • | • | • | • | • | .491 | •492 | • 492 |
| | | | | | | | | |
| | | | | $R_{\mathbf{w}}^2$ | | | | |
| K _o | 7500 | 10000 | 12500 | 15000 | 17500 | 20000 | 22500 | 25000 |
| Luz | | | | | | | | |
| 5 | .867 | .895 | .902 | .900 | .894 | | | • |
| 10 | .867 | .899 | .912 | .914 | .912 | • | • | |
| 15 | .865 | .900 | .917 | .923 | .924 | - | · · | `. |
| 20 | .861 | .898 | .918 | .927 | 930- | 931 | .929 | .926 |
| 25 | .855 | .893 | .914 | .925 | .331 | •933 | .934 | .932 |
| 30 | • | • | ; / | • | | .931 | • 933 | •933 |
| | | | , |) | | | | |

Fig. 5.11 The response of the R^2 -criteria to K_0 (1/(s · mm)) and L_{117} (mm) at Stadarforsen. (See chapter 5.4; 5.4.

5.4.3 The response of the
$$R^2$$
-criteria to K and L uz

K_o affects the top flow recession rate and L_{uz} the level, at which this recession rate is activated. A great improvement of the R^2 -criteria can be seen here. It is only the R_3^2 -criterion that is not improved when increasing K_o and L_{uz}. (Fig. 5.11).

A test plotting was made at:

$$K_o = 22 500 1/s \cdot mm,$$

 $L_{uz} = 25 mm.$

The plotting corresponds to the information available through the \mathbb{R}^2 -criteria. The result is a better overall fit, especially at high flows but perhaps there is some deterioration at low flow.

5.4.4 The response of the R^2 -criteria to K_0 and K_1

In fig. 5.12 we have got an example of how the snowmelt (R_1^2) class practically governs the R_w^2 -criterion. A test plotting was made at the optimum of the R_w^2 -criterion.

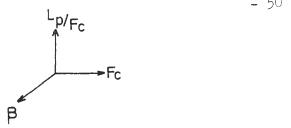
$$K_0 = 16 500 \text{ l/s} \cdot \text{mm},$$

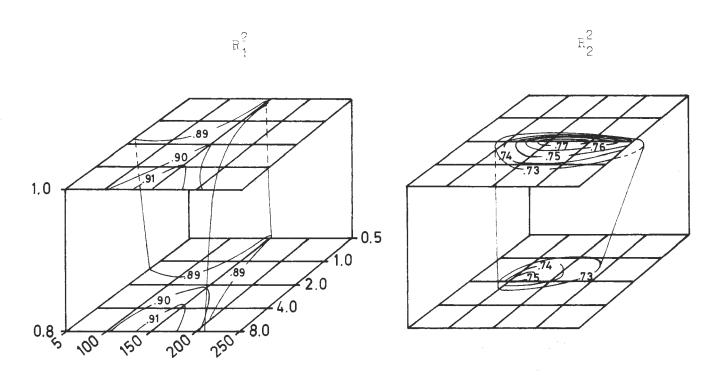
 $K_1 = 3 500 \text{ l/s} \cdot \text{mm}.$

It showed out to be somewhat inferior to the original plotting. The difference, however, was considered to be of minor importance.

Fig. 5.12 The response of the R²-criteria to K_0 (1/(s · mm)) and K_1 (1/(s · mm)) at Stadarforsen. (See next page)

| R ² | | | | | | | |
|---|--|--|---|---|---|---------------|---------------|
| Ko | 8500 | 10500 | | 14500 | 16550 | 185 [| 20500 |
| ĸ ₁ | | | | | | | |
| 1500 | .820 | .360 | ,851 | r.ē91 | .694 | . \ | |
| 2500 | .819 | .858 | 879 | \b90 | .694 | | /. |
| 3500 | .819 | .857 | 879 | .689 | .393 | .893 | 1890 |
| 4500 | .820 | .857 | .878 | .889. | .893 | .893 | 890 |
| 5500 | .821 | .857 | .878 | ,888, | .892 | . / | <i>'</i> . |
| | | | | | | | |
| | | | R | 2 | | | |
| K _O | 8500 | 10500 | | 14500 | 16500 | 18506 | 20500 |
| ĸ | | | | | | | |
| 1500 | .812 | .802 | .785 | .765 | .744 | | • |
| 2500 | .837 | -834 -834 | .823 | 809 | .794 | | |
| 3500 | .835 | .836 | 831 | .822 | .811 | .800 | .789 |
| 4500 | .824 | .827 | .826 | 820 | .812 | .803 | .794 |
| 5500 | .810 | .816 | .813 | 809 | .802 | • | |
| | | | | | | | |
| . 2 | | | | | | | |
| | | | R | 2 | | | |
| K o | 8500 | 10500 | R 12500 | 2 3 14500 | 16500 | 18500 | . 20500 |
| K _o | 8500 | 10500 | | | 16500 | 18500 | 20500 |
| K ₁ | . 8500 | | 12500 | | 16500 .472 | 18500 | 20500 |
| K ₁ | .380 | .414 | 12500 | 14500 | .472 | 18500 | 20500 |
| K ₁ 1500 2500 | .380 | .414 | .440 | .458 .479 | .472 | | |
| K ₁ | .380 | .414 | .440 .475 | 14500 .458 .479 .549 | .472 .478 | · - 550_ | · · 551 |
| K ₁ 1500 2500 3500 | .380 | .414 | .440 | .458 .479 | .472 .478 .549 | | |
| K ₁ 1500 2500 3500 4500 | .380 .452 .528 | .414 | .440 .475 .550 | .458 .479 .549 | .472 .478 .549 | · - 550_ | · · 551 |
| K ₁ 1500 2500 3500 4500 | .380 .452 .528 | .414 | .440 .475 .550 | .458 .479 .549 | .472 .478 .549 | · - 550_ | · · 551 |
| K ₁ 1500 2500 3500 4500 | .380 .452 .528 | .414 | .440 .475 .550 .563 | .458 .479 .549 .549 | .472 .478 .549 | · - 550_ | · · 551 |
| K ₁ 1500 2500 3500 4500 5500 | .380 .452 .526 .581 | .414 .466 .543 | .440 .475 .550 .563 | .458 .479 .549 .542 | .472 .478 .549 .557 | .5550 | |
| K ₁ 1500 2500 3500 4500 5500 | .380 .452 .526 .581 | .414 | .440 .475 .550 .563 | .458 .479 .549 .542 | .472 .478 .549 .557 | .5550 | |
| K ₁ 1500 2500 3500 4500 5500 | .380 .452 .526 .581 | .414 .466 .543 .3775 _549 | .440 .475 .550 .563 | .458 .479 .549 .542 | .472 .478 .549 .557 | .5550 | |
| K ₁ 1500 2500 3500 4500 5500 | .380 .452 .526 .581 .564 | .414 .466 .543 .577 .549 | .440 .475 .550 .563 .547 R ₂ 12500 | .458 .479 .549 .542 | .472 .478 .549 .557 | .5550 | |
| K ₁ 1500 2500 3500 4500 5500 | .380 .452 .526 .581 .564 .8500 | .414 .466 .543 .3775 _549 | 12500 .440 .475 .550 .563 .547 R ² .7 12500 | .458 .479 .549 .542 .542 .14500 | .472 .478 .549 .557 .539 | .5550 .5555 . | |
| K ₁ 1500 2500 3500 4500 5500 K ₀ K ₁ 1500 2500 3500 | .380 .452 .526 .581 .564 .564 .883 .883 | .414 .466 .543 .577 .549 | 12500 .440 .475 .550 .563 .547 R. 12500 .916 .917 .917 | 14500 .458 .479 .549 .549 .542 .14500 .920 .922 | .472 .478 .549 .557 .539 16500 .921 .923 .924 | | |
| K ₁ 1500 2500 3500 4500 5500 | .380 .452 .526 .581 .564 .8500 | .414 .466 .543 .3775 _549 10500 | 12500 .440 .475 .550 .563 .547 R ² .7 12500 | .458 .479 .549 .542 .542 .14500 | .472 .478 .549 .557 .539 | | |





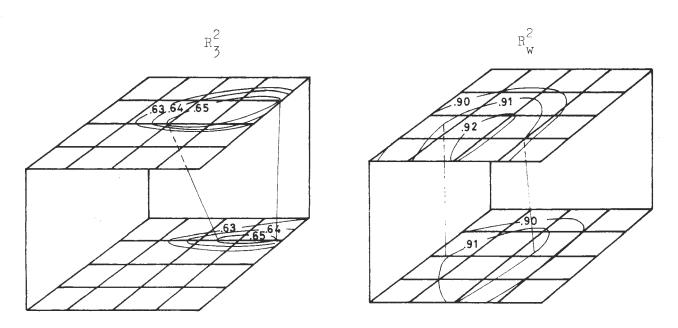


Fig. 5.13 The response of the ${
m R}^2$ -criteria to Fc (mm), ${
m L_p/Fc}$ and β at Stadarforsen. (See chapter 5.4; 5.4.5)

| ŝ | 0.5 | 1.0 | 2.0 | 4.0 | 8.0 |
|-------------------|-------|-------|----------|------|---------------|
| ៊ិ _{នេះ} | | | | | |
| 0.80 | .889 | . 893 | 3 .905 | 912 | 2 ~ 208 |
| 0.85 | .385. | .892 | z \v.903 | .913 | 193 |
| 0,90 | .373 | .87 | 88, | 2996 | - |
| 0.95 | .843 | .843 | 2 .848 | 3E | 2.876 |
| 1.00 | .800 | .796 | .799 | .818 | .833 |

 R_2^2

| ß | 0.5 | 1.0 | 2.0 | 4.0 | 5.0 |
|------|------|------|------------|-------|------|
| Csf | | | | | |
| 0.80 | .284 | .719 | 837 85p | \.770 | .684 |
| 0.85 | .262 | -707 | 85p | 1.791 | .696 |
| 0.90 | .235 | .699 | 858 | 808 | .713 |
| 0.95 | .205 | .684 | .855 | 1. 1 | |
| 1.00 | .151 | .657 | 11 850 | 1820 | -732 |

R²

| β | 0.5 | 1.0 | 2.0 | 4.0 | 8.0 |
|----------------------------|--------------|---------|-------------------|------|-------|
| $\mathbf{C}_{\mathtt{sf}}$ | | | | | |
| 0.80 | , 518 | .519 | .525 | .440 | .254 |
| 0.85 | •525/ | TOPP TO | .541 | -473 | .310 |
| 0.90 | -516 | 5,585 | \$55 | .503 | • 355 |
| 0.95 | •505 •505 | 584 | .5 \ a | .522 | •397 |
| 1.00 | 498. | W 574 | 554 | 53/ | .430 |

 $R_{\rm w}^2$

5.14 The response of the x^2 -criteria to 0 and x at Stadar-forsen. (See chapter 5.4; 5.4.6)

5.4.5 The response of the
$$R^2$$
-criteria to Fc, L_p /Fc and g

The danger of letting the R_w^2 -criterion define the parameter optimum is accentuated in fig. 5.13. A test plotting was made at:

Fc = 150 mm
$$L_{p} = 150 mm$$

$$\beta = 4$$

This is the R_w^2 -optimum. The model now underestimates γ -flow. From the response surface it is clear that the R_{ρ}^2 -criterion was deteriorated by this modification of the parameters. This gives an unacceptable error in the accumulated flow after the four calibration years.

The R_{sum} -criterion (chapter 5.1), however, has its optimum at:

$$Fc = 150 \text{ mm}$$

$$L_{p} = 150 \text{ mm},$$

$$\beta = 2.$$

$$\beta^{T} = 2.$$

which is very close to the original setting.

5.4.6 The response of the R^2 -criteria to C_{sf} and β

The P_{sum}-criterion (chapter 5.1) shows optimum (compare fig. 5.14) at:

$$\beta = 2.0,$$

$$C_{sf} = 0.9.$$

No test plotting was made, because the original parameter values are close to this optimum. and further more the test plotting of chapter 5.4.5 showed no improvement of the hydrograph.

According to fig. 5.15 C seemed to be a bit too small, and a test plotting was made at:

$$T_0 = 0^{\circ}C,$$
 $C_0 = 2.3 \text{ mm/}(^{\circ}C \cdot \text{ day}).$

It shows a small improvement.

R2

 $\mathbb{R}^2_{\mathbf{w}}$

 \mathbb{R}_1^2

R_2^2

R_3^2

\mathbb{R}^2_{ω}

```
      Crfr
      0.00
      0.05
      0.10
      0.20
      0.40
      0.80

      Cwh
      0.00
      .919
      .919
      .919
      .919
      .919
      .919

      0.05
      .929
      .934
      .934
      .929
      .923
      .919

      0.10
      .935
      .933
      .950
      .923
      .907
      .888

      0.15
      .935
      .923
      .917
      .903
      .882
      .

      0.20
      .929
      .907
      .898
      .879
      .851
      .
```

Fig. 5.15 The response of the x²-criteria to C_{wn} and C_{rfr} at Stadarforsen. (See chapter 5.4; 5.4.8).

5.4.8 The response of the R2-criteria to the and rir

The settings of $C_{\bf rfr}$ and $C_{\bf wn}$ to 0 were assumed to be physically impossible and of only theoretical interest. An optimum setting then seemed to be (fig. 5.16):

$$C_{rfr} = 0.05,$$
 $C_{wh} = 0.05.$

A plotting was made at this point. The test plotting managed to center the spring floods better than the original plotting and was therefore considered to be better than the original one.

5.5 Results of the study

It is obvious that the R_W^2 -criterion is not a good criterion of fit for our purposes. The snowmelt period governs the behaviour of the R_W^2 -criterion too much. For example, the β -parameter of Stadarforsen (and to some extent the one of Kultsjön too) is badly optimized by the R_W^2 -criterion.

Another disadvantage of the studied criteria is the R_3^2 -criterion. It is disturbed by the fact that different parameter settings give different classifications of data. Both the initial variance and the sum of the squared residuals may be greatly changed by this phenomenon. This could lead to a change in R_3^2 , not from a change of fit, but film a rearrangement of the data available.

In order to develop an acceptable criterion of fit the sum of the $\rm R_1^2$, the $\rm R_2^2$ and the $\rm R_3^2$ -criteria was also studied. The weakness of $\rm R_3^2$ described above, however, does influence this criterion too.

To overcome this drawback it is suggested that the classification of data should not be changed during comparison of different parameter settings.

| Parameter | Original setting | R ₁ -optimum | R ₂ -optimum | R ₃ ² -optimum | R -optimum | R _w ² -optimwn |
|--|---------------------|-------------------------|-------------------------|--------------------------------------|------------|--------------------------------------|
| $\int_{\mathbb{K}_{2}} (1/(s \cdot mm))$ | 350 | 300 | 500 | 350 | 350 | 35 ⁰ |
| Cperc (mm/day) | 1.0 | 1.0 | 1.5 | 1.0 | . 1.0 | 1.0 |
| $\left(K_1 \left(1/(s \cdot mn) \right) \right)$ | 3500 | 1500 | 3500 | 3500 | 3500 | 3500 |
| (days/m ³) | 0.0000 | 0.0000 | 0.0005 | 0.0010 | 0.0000 | 0.0000 |
| max (days) | 6 | 5 | 7 | 5 | 5 | 5 |
| $\int K_{o} (1/(s \cdot mm))$ | 12500 | 25000 | 25000 | 7500 | 22500 | 22500 |
| Luz (mm) | 15 | 30 | 25 | 5 | 25 | 25 |
| $\int_{0}^{\infty} \left(1/(s \cdot mm) \right)$ | 12500 | 16500 | 8500 | 8500 | 14500 | 16500 |
| $\left(\mathbb{K}_{1}^{\prime} \left(1/(\mathbf{s} \cdot \mathbf{m}) \right) \right)$ | 3500 | 3500 | 2500 | 4500 | 4500 | ا غرام کا غرام کا |
| √Fe (mm) | 1 50 | 150 | 1 50 | 150 | 150 | 150 |
| L _p /Fc | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 | 1.0 |
| $\left\{ egin{aligned} \mathbf{L}_{\mathbf{p}}/\mathbf{Fc} \\ \mathbf{eta} \end{aligned} ight.$ | 1.5 | 8.0 | 2.0 | 1.0 | 2.0 | 4.0 |
| ∫B | . 1.5 | 8.0 | 2.0 | 1.0 | 2.0 | 4.0 |
| $c_{ m sf}$ | 0.90 | 0.85 | 0.95 | 0.85 | 0.90 | 0.85 |
| ∫T _o (°C) | 0.0 | J. O ,, | 0.5 | - 0.5 | 0.0 | 0.0 |
| C_{\circ} (mm/($^{\circ}$ C · day)) | 2.0 | 2.3 | 2.6 | 1.7 | 2.3 | 2.3 |
| $\int_{\mathrm{C_{wh}}}$ | 0.05 | 0.05 | 0.10 | 0.05 | 0.10 | 0.05 |
| Crfr | 1.0 | 0.05 | 0.05 | 1.0 | 0.05 | 0.05 |

Table 5.2 The optimum parameter settings of Stadarforsen as judged by the different criteria of fit.

For comparison the original parameter setting (the optimum of an 8 year period as judged by the calibraters) is also printed in this table.

KULTSJÖN

| | Parame ter | Original setting | R ₁ opti- | R ₂ opti- | R ² opti- | R opti- | R _w opti- |
|----|-----------------------------|------------------|----------------------|----------------------|----------------------|---------|----------------------|
| | F ₂ (#/(s ~ mm)) | 300 | 600 | 200 | 600 | 450 | 450 |
| ÷, | (nm/day) | 1,3 | 3.6 | 2. | 2.7 | 2.4 | 2.6 |
| | K, (1/(s · mm)) | 4000 | 3000 | 3000 | 6000 | 3000 | 3 000 |
| : | Croute (day s/m3) | 0.00103 | 0.0005 | 0.001 | O | 0.001 | 0.0005 |
| : | P _{max} (days) | 2 | 2 | 2 | 3 | 2 | 2 |
| | Fe (mm) | 150 | 200 | 200 | 100 | 200 | 200 |
| Ì | I _p /Fe | 1.0 | 0.6 | 0.6 | 0.6 | 0.6 | 0.6 |
| | L _p /Fc β | 3.0 | 1.0 | 4.0 | 2.0 | 4.0 | 2.0 |
| | ∫β | 3.0 | 1.0 | 4.0 | 2.0 | 4.0 | 2.0 |
| | Csf | 1.23 | 1.2 | 1.1 | 1.0 | 1.1 | 1.1 |
| | To (°C) | 0.5 | - 0.5 | 0.5 | 0.0 | 0.0 | 0.0 |
| 1 | (c (mm/(°C • day)) | 3.2 | 2.0 | 3.5 | 3.8 | 2.9 | 2.6 |
| | C _{wh} | 0.05 | 0,05 | 0.05 | u.05 | 0.05 | 0.05 |
| , | Crfr | 1.0 | 1.0 | 0.05 | 0.05 | 0.4 | 1,0 |

Table 5.3 The optimum parameter settings of Kultsjön as judged by the different criteria of fit.

For comparison the original parameter setting (the optimum of an 8 year period as judged by the calibrators) is also printed in this table.

The optimum parameter settings, as described by the different R^2 -criteria and the R_{sum} -criterion, may be studied in tab. 5.2 and 5.3, where they are compared with results from calibrations by visual inspection. Note that the HBV-model is usually calibrated during 8-year periods, but due to the computer capacity only 4-year periods were used in the study of the response surfaces of the R^2 -criteria. We see that the R_{sum} -criterion is mostly closer to the original setting than the R^2 -criterion (tab. 5.4).

In Kultsjön, however, any studied parameter optimum suggested by any of the criteria did not give better hydrographs than the originally plotted one. Possible explanations to this are the bad quality of both the runoff data and the climate data and the incompleteness of the model type used (the lack of a K_{o} -parameter).

In Stadarforsen the R_{sum} -criterion agrees with the visual inspection surprisingly well. If some sort of fixed classification manages to make the R_3^2 -criterion more reliable, it is obvious that the HBV-model could be automatically calibrated in Stadarforsen.

Whether the model can be automatically calibrated for any catchment, is a much harder question. This study covers only two catchments and furthermore only four years of each one.

The impression of the author is that the R_{sum}-criterion or some other linear combination of the R²-criteria might be the basis of a useful criterion of fit. Other quantities, such as the sum of the residuals and the ratio of over- or underestimations of the hydrograph, may perhaps take part in a criterion of fit too, since these two quantities are often used during the subjective calibration.

| | Svalariorsen | | | | ,Lns; | (St |
|-------------------------|--------------|----------------|--|--|-------------|----------------|
| | ** *50111 | E _w | | | sun | 3 ² |
| <u>.</u> | 2 | × | | | 30 | Ж |
| nere | 4. | 1 22 | | | _£ | |
| K, | - | ¥ | | | X | x |
| croute | *= | X | | | X | |
| Croute Smax | J. | i | | | D. | 77 - |
| K | Х | Х | | | - | - |
| Luz | X | 21 | | | 80 * | _ |
| К. О | 25 | | | | | *** |
| К ₁ | | Ж. | | | - | x |
| Fe | 2.5 | X | | | X | x |
| L_{p}/Fc | 32 | X | | | X | <i>3.</i> |
| L _p /Fc 3 | Ā | | | | X | |
| j. | Х | | | | 34 | |
| C sf | 75 | | | | X | Y_ |
| To | ¥ | ĸ | | | x | X |
| Co | M. | 22 | | | ĸ | *** |
| C wh | | - | | | K | <u> 25</u> |
| Crîr | | 9.7 | | | | 30 |

Table 5.4 A comparison between the $R_{\rm sum}$ and $\Gamma_{\rm s}^{7}$ emirania of dit. The oritorian thich has its optimal large to the original parameter setting is marked with a cross.

6. CONCLUSIONS

The residuals of the HBV-model are neither independent nor stationary distributed during the year. Yet this has been assumed by many calibrators of hydrological models. A way to get closer to these assumptions is to base a classification of the calibration data on the different processes governing the discharge and to consider each class to be a separate set of residuals. By doing this we do not get rid of the autocorrelation, but the residuals become more stationary distributed. In fact it is impossible to get rid of the autocorrelation of the model residuals, since one single climate measurement error affects the level of the model storage and thereby the discharge during a series of days.

Knowing that a classification helps in making the residuals more stationary, the R_{i}^{2} -criterion of fit (chapter 5.1) was computed for each class. The sum of these R_{i}^{2} -criteria (the R_{sum} -criterion) showed out to be a better criterion of fit than the formerly used R_{w}^{2} -criterion. Concerning the possibility of automatic calibration of the HBV-model at any catchment, data of good quality must be demanded. There must also be a sufficient number of degrees of freedom in the model. It might otherwise compensate an unability to follow the observed hydrograph by producing a too damped hydrograph, overestimating low flows and underestimating high ones.

If these demands are fullfilled, the R_{sum} -criterion gives a better representation of the goodness of fit than the R_{w}^2 -criterion. The response surfaces had mostly a regular elliptic shape. Therefore it seems plausible that an optimization algorithm such as Rosebrock's (1960) method or Powell's (1964) method with slight modifications may perform acceptably.

The demand above of many degrees of freedom contains a dilemma. If a model is equipped with a sufficient number of degrees of freedom, it will be able to reconstruct almost any discharge record from any climate record. But the headpoint in making a model is not to make

it complex in order to fit the calibration period only, (since this is no guarantee for fit during other periods), but to make it simple and yet fit both the calibration period and the independent periods.



APPENDIX A

The distributions of the residuals (differences between the computed and the recorded hydrographs) are shown below. Histograms showing the residuals both separated and not separated by the MSC (chapter 4.1) are plotted.

A description of the method used when constructing these histograms can be found in chapter 4.2. The prescribed minimum period duration is explained in chapter 4.4.

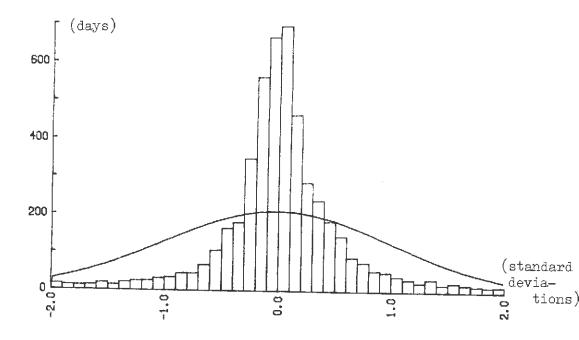


Fig. A.1 Histogram showing the residuals of Stadarforsen 61.10.01 - 76.03.31.

Prescribed minimum period duration: 1 day.

Mean = -589 1/s.

Standard deviation = 22 503 1/s.

Number of residuals = 5 273.

Number of exceeding residuals (NER) = 337.

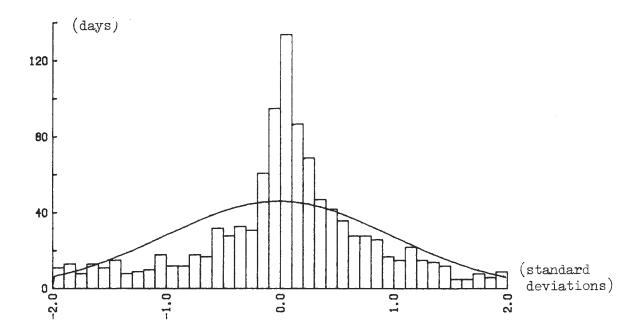


Fig. A.2 Histogram showing the snowmelt residuals of Stadarforsen, 61.10.01 - 76.03.31.

Prescribed minimum period duration: 1 day.

Mean = 1 385 1/s.

Standard deviation = 41 431 1/s.

Number of residuals = 1 156.

NER = 76.

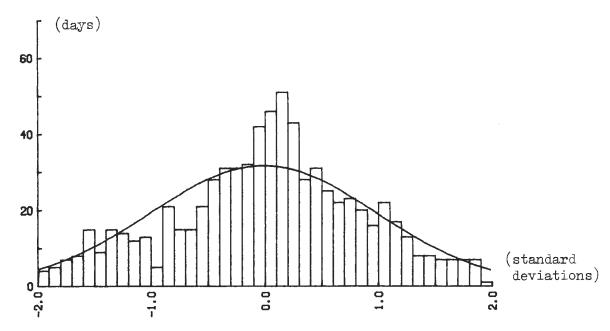


Fig. A.3 Histogram showing the snowmelt residuals of Stadarforsen, 61.10.01 - 76.03.31.

Prescribed minimum period duration: 5 days.

Mean = -4 645 1/s.

Standard deviation = 48 485 1/s.

Number of residuals = 794.

NER = 49.

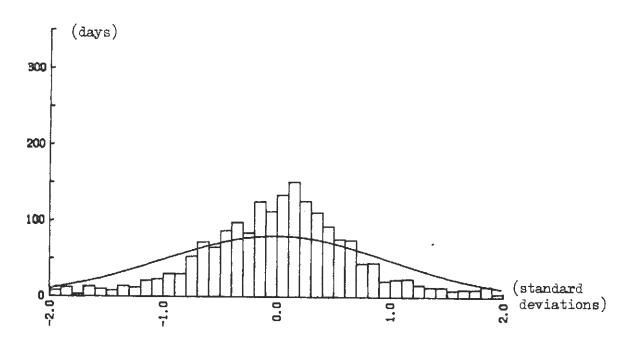


Fig. A.4 Histogram showing the γ-flow residuals of Stadarforsen 61.10.01 - 76.03.31.
Prescribed minimum period duration: 1 day
Mean = 16 l/s.
Standard deviation = 17 553 l/s.

Number of residuals = 2 008.
NER = 116.

(standard deviations)

Fig. A.5 Histogram showing the γ-flow residuals of Stadarforsen 61.10.01 - 76.03.31. Prescribed minimum period duration: 5 days. Mean = -590 l/s.

Standard deviation = 18 185 1/s.

Number of residuals = 1 650.

NER = 94.

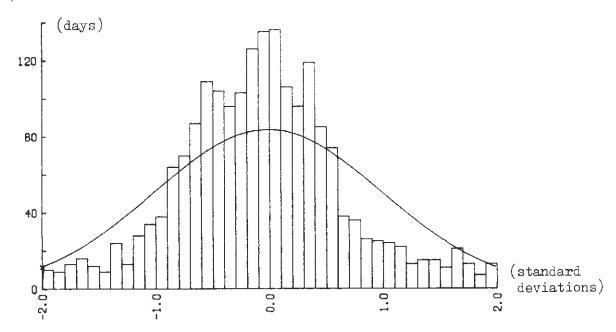


Fig. A.6 Histogram showing the low flow residuals of Stadarforsen 61.10.01 - 76.03.31.

Prescribed minimum period duration: 1 day.

Mean = -743 1/s.

Standard deviation = 5 629 1/s.

Number of residuals = 2 097.

NER = 102.

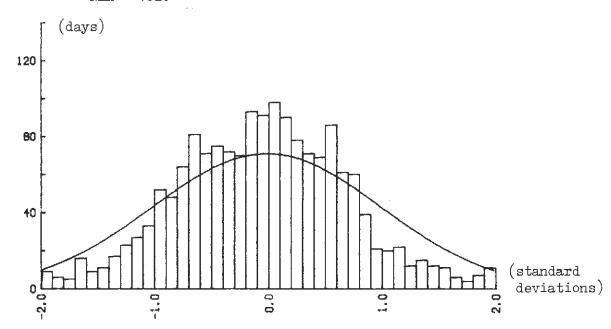


Fig. A.7 Histogram showing the low flow residuals of Stadarm forsen 61.10.01 - 76.03.31.

Prescribed minimum period duration: 5 days.

Mean = $1 \cdot 188 \cdot 1/s$.

Standard deviation = 4 393 1/s.

Number of residuals = 1 780.

NER = 114.

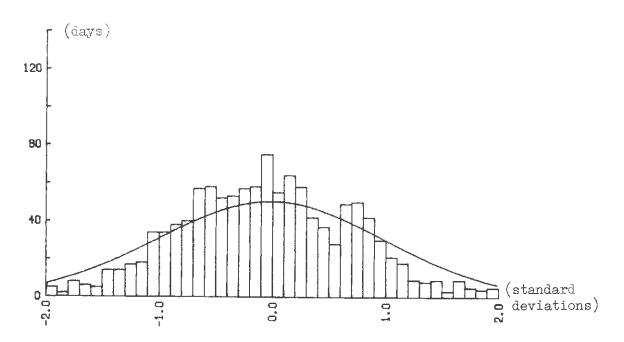


Fig. A.8 Histogram showing the low flow residuals of Stadarforsen 61.10.01 - 76.03.31.

Prescribed minimum period duration: 20 days

Mean = -1 578 1/s.

Standard deviation = 3 890 1/s.

Number of residuals = 1 260.

NER = 69.

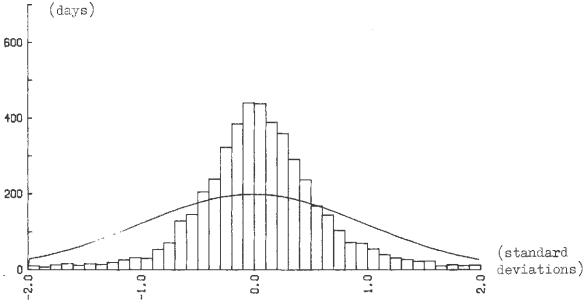


Fig. A.9 Histogram showing the residuals of Kultsjön 62.10.01 - 76.05.18.

Prescribed minimum period duration: 1 day.

Mean = 374 1/s.

Standard deviation = 16 905 1/s.

Number of residuals = 4 977.

NER = 274.

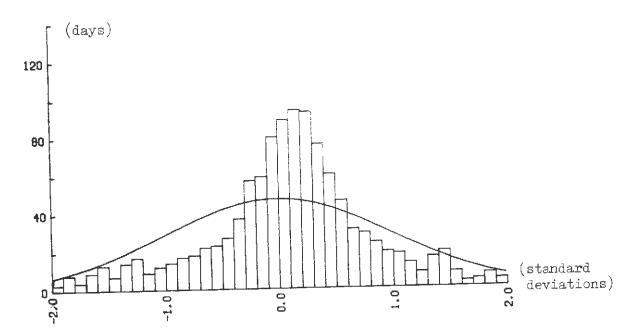


Fig. A.10 Histogram showing the snowmelt residuals of Kultsjön 62.10.01 - 76.05.18.

Prescribed minimum period duration: 1 day

Mean = $-545 \, 1/s$.

Standard deviation = 30 198 1/s.

Number of residuals = 1 185.

NER = 74.

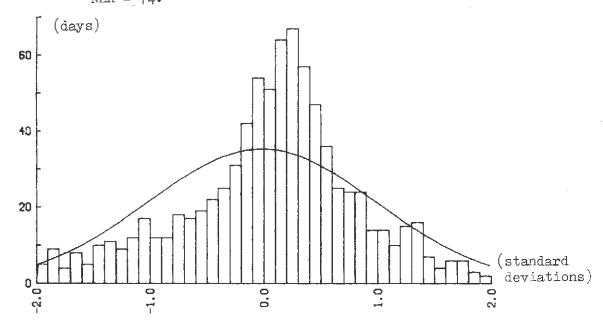


Fig. A.11 Histogram showing the snowmelt residuals of Kultsjön 62.10.01 - 76.05.18.

Prescribed minimum period duration: 5 days.

Mean = -2400 1/s.

Standard deviation = 33 605 1/s.

Number of residuals = 884.

NER = 50.

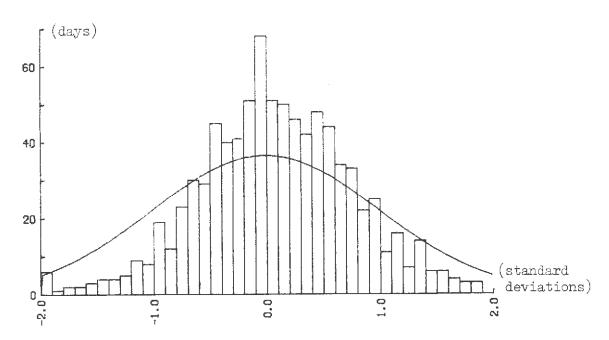


Fig. A.12 Histogram showing the γ -flow residuals of Kultsjön 62.10.01 - 76.05.18.

Prescribed minimum period duration: 1 day.

Mean = $411 \, 1/s$.

Standard deviation = 14 652 1/s.

Number of residuals = 914.

NER = 47.

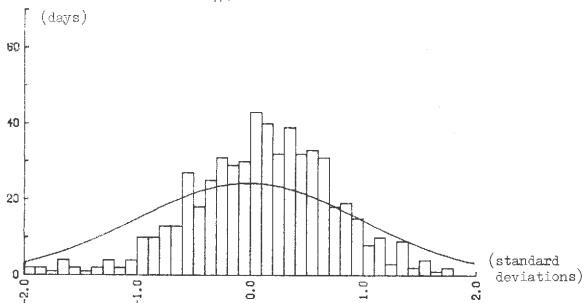


Fig. A.13 Histogram showing the γ -flow residuals of Kultsjön 62.10.01 - 76.05.18.

Prescribed minimum period duration: 5 days.

Mean = 1.178 1/s.

Standard deviation = 16 067 1/s.

Number of residuals = 607.

NER = 36.

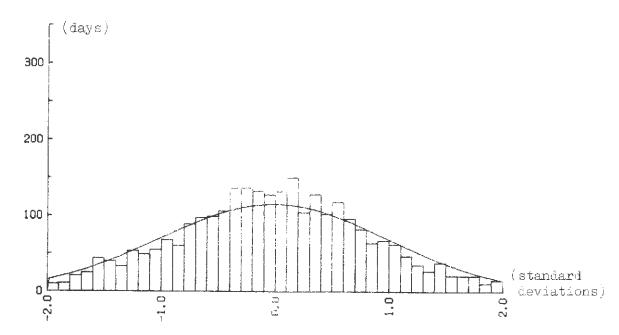


Fig. A.14 Fistogram showing the low flow residuals of Kultsjön 62.10.01 - 76.05.18.

Prescribed minimum period duration: 1 day.

Mean = $725 \, 1/s$.

Standard deviation = 7 068 1/s.

Number of residuals = 2 876.

NER = 145.

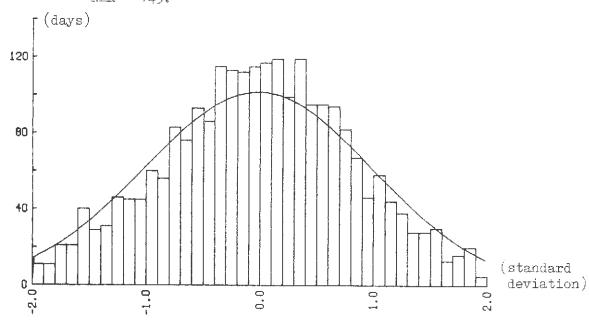


Fig. A.15 Histogram showing the low flow residuals of Kultsjön 62.10.01 - 76.05.18.

Prescribed minimum period duration: 5 days.

Mean = $530 \pm /s$.

Standard deviation = 6 863 1/s.

Number of residuals = 2 545.

NER = 123.

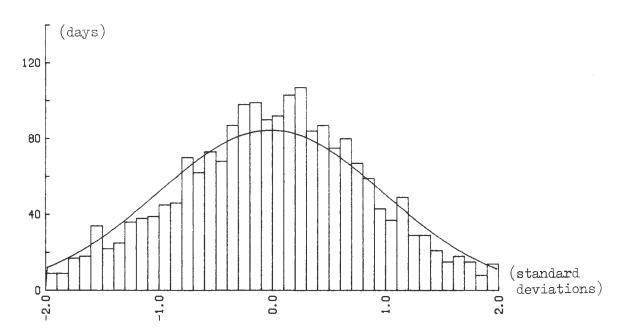


Fig. A.16 Histogram showing the low flow residuals of Kultsjön 62.10.01 - 76.05.18.

Prescribed minimum period duration: 20 days.

Mean = 370 1/s.

Standard deviation = 6 637 1/s.

Number of residuals = 2 117.

NER = 100.



Appendiz B

nx

LIST OF SYMBOLS

| B | maximum base in the transformation function |
|----------------------------------|---|
| $\mathbb{B}_{	extsf{q}}$ | actual base in the transformation function |
| Co | degree-day melt factor |
| $^{ m C}_{ m perc}$ | percolation capacity |
| $^{	ext{C}}_{	t rfr}$ | refreezing coefficient |
| $^{\mathtt{C}}_{\mathtt{route}}$ | parameter in the transformation function |
| Csf | snowfall correction factor |
| $^{\mathrm{C}}$ wh | water holding capacity of snow |
| Ea | actual evaporation |
| Ep | potential evaporation |
| Fc | maximum soil moisture capacity in the model |
| F ₀ 2 | initial variance |
| Ko | storage discharge parameter of the upper zone |
| ^K 1 | slow drainage storage discharge parameter of the upper zone |
| K ₂ | storage discharge prameter of the lower zone |
| L _p | limit for potential evaporation |
| Luz | limit for slow drainage of the upper zone |
| M | ${\tt snowmelt}$ |
| MSC | mechanism separation criterion |
| n | total number of observations in a class |
| N | number of observations in a continous period in a class |
| NER | number of residuals not contained in the histo- gram of the estimated density function |
| Ν _τ | total number of observations of $R(\tau)$ |
| $^{ m N}$ j | duration of period j |
| | |

sum of autocorrelation coefficients

```
P
             precipitation
P_{\text{corr}}
             rainfall correction factor
Plapse
             area elevation correction c. precipitation
             probability
p;
             part of the lower zone representing wet areas
\mathbf{Q}_{\mathrm{O}}
             runoff generated from the upper zone
Q
             slow drainage runoff generated from the upper zone
             runoff generated from the lower zone
Q_{\gamma}
             computed runoff
Q<sub>C</sub>
Q<sub>g</sub>
             total generated runoff
             recorded runoff
             mean of recorded runoff
             criterion of fit
             criterion of fit (R_1^2 + R_2^2 + R_3^2)
\mathbb{R}_{\mathtt{sum}}
                               (the material as a whole)
                                 (snowmelt)
                                 (y-flow)
                                 (low flow)
R(\tau)
             autocovariance with time step T
\hat{R}(\tau)
             estimation of the autocovariance
\hat{R}_{j}(\tau)
             estimated autocovariance of residuals separated by t
               days for the j:th continuous period
S
             standard deviation
S.
              ottom storage under the snowpack
             storage in the lower zone of the model
S
Ss
             storage of snow in the catchment
             soil moisture storage in the model
s_{uz}
             storage in the upper zone of the model
             temperature
             general temperature correction
```

| $^{	extsf{T}}$ lapse | area elevation correction of temperature |
|------------------------|---|
| t | time |
| ${	t t}_{	extstyle j}$ | starting time for the j:th period |
| U | test variable |
| Var(X) | variance of the stochastic variable X |
| X | a residual regarded as a stochastic variable |
| \overline{X} | mean value of the residuals |
| β | parameter of the soil moisture zone |
| Υ | indicates rain or recession succeeding rain or snowmelt |
| μ | mean value |
| σ | standard deviation |
| τ | time step |

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